

# The $rp$ -Process in Neutrino-driven Winds

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## ABSTRACT

Recent hydrodynamic simulations of core-collapse supernovae with accurate neutrino transport suggest that the bulk of the early neutrino-heated ejecta is proton rich, in which the production of some interesting proton-rich nuclei is expected. As suggested in recent nucleosynthesis studies, the rapid proton-capture ( $rp$ ) process takes place in such proton-rich environments by bypassing the waiting point nuclei with the  $\beta^+$ -lives of a few minutes via the faster capture of neutrons continuously supplied from the neutrino absorption by protons. In this study, the nucleosynthesis calculations are performed with the wide ranges of the neutrino luminosities and the electron fractions ( $Y_e$ ), using the semi-analytic models of proto-neutron star winds. The masses of proto-neutron stars are taken to be  $1.4 M_\odot$  and  $2.0 M_\odot$ , where the latter is regarded as the test for somewhat high entropy winds (about a factor of two). For  $Y_e > 0.52$ , the neutrino-induced  $rp$ -process takes place in many wind trajectories, and the  $p$ -nuclei up to  $A \sim 130$  are synthesized with interesting amounts. However,  $^{92}\text{Mo}$  is somewhat underproduced compared to those with similar mass numbers. For  $0.46 < Y_e < 0.49$ , on the other hand,  $^{92}\text{Mo}$  is significantly enhanced by the nuclear flows in the vicinity of the abundant  $^{90}\text{Zr}$  that originates from the  $\alpha$ -process at higher temperature. The nucleosynthetic yields are averaged over the ejected masses of winds, and further the  $Y_e$  distribution predicted by the recent hydrodynamic simulation of a core-collapse supernova. Comparison of the mass- $Y_e$ -averaged yields to the solar compositions implies that the neutrino-driven winds can be potentially the origin of light  $p$ -nuclei up to  $A \sim 110$ , including  $^{92,94}\text{Mo}$  and  $^{96,98}\text{Ru}$  that cannot be explained by other astrophysical sites. This parametric study suggests that the neutrino-induced  $rp$ -process takes place in *all* core-collapse supernovae, and likely in collapsar jets or disk winds formed around a black hole. Although the quantitative prediction of  $rp$ -processed abundances requires future detailed multi-dimensional hydrodynamic simulations with accurate neutrino transport, the current investigation will serve unique constraints to the fluid dynamics of the early supernova ejecta.

*Subject headings:* nuclear reactions, nucleosynthesis, abundances — stars: abundances — stars: neutron — supernovae: general

## 1. Introduction

The rapid proton-capture ( $rp$ ) process of nucleosynthesis is expected to take place in proton-rich compositions with sufficiently high temperature (Wallace & Woosley 1981), which leads to the production of proton-rich isotopes beyond iron. This is an analogous phenomenon to the rapid neutron-capture ( $r$ ) process in neutron-rich compositions,

which accounts for the production of about half of the species heavier than iron (see Wanajo & Ishimaru 2006b, for a recent review). A major difference between these two processes is the presence of the Coulomb barrier for proton capture reactions. This limits the requisite temperature for this process to a small range,  $\sim 1 - 3 \times 10^9 \text{ K}$ , in which the proton capture proceeds during short time compared to the relevant  $\beta^+$ -decay lifetimes

without substantial photodisintegrations. To date the thermonuclear explosions of hydrogen-rich material on accreting neutron stars (X-ray bursts) have been considered to be the promising astrophysical site associated to the occurrence of *rp*-process (e.g., Schatz et al. 1998; Koike et al. 1999; Brown et al. 2002; Woosley et al. 2004). However, little amount of the nucleosynthetic product is expected to be ejected, whose contribution to the Galactic chemical evolution is likely to be negligible.

Recent hydrodynamic studies of core-collapse supernovae that take the accurate neutrino transport into account have shown that the bulk of the neutrino-heated ejecta during the early phase ( $\lesssim 1$  s) is *proton-rich* (Liebendörfer et al. 2003; Pruet et al. 2005; Buras et al. 2006; Kitaura, Janka, & Hillebrandt 2006; Fröhlich et al. 2006a). Given this proton richness in the innermost ejecta is the general characteristic, one might think that core-collapse supernovae provide suitable physical conditions for the *rp*-process. If this is true, the study of *rp*-process in core-collapse supernovae will be of special importance, which no doubt eject the nucleosynthetic products and thus contribute to the Galactic chemical evolution. However, there are a number of nuclei with the  $\beta^+$ -lives of a few minutes on the *rp*-process path. These “waiting point” nuclei inhibit the production of heavy proton-rich nuclei beyond the iron-group in core-collapse supernovae (Pruet et al. 2005). The first waiting point nucleus encountered soon after the abundant  $^{56}\text{Ni}$  is  $^{64}\text{Ge}$ . The half life of its  $\beta^+$ -decay is 1.06 min, which is obviously longer than the dynamic timescale of the innermost ejecta of a core-collapse supernova ( $< 1$  s).

The situation changes dramatically, however, when neutrino-induced reactions are included in the nucleosynthesis calculations. In fact, recent studies by Fröhlich et al. (2006a,b), Pruet et al. (2006), and Wanajo (2006) have shown that the  $\beta^+$ -waiting points are bypassed via neutron capture reactions even in proton-rich environments. This is due to the continuous supply of neutrons from the anti-electron neutrino absorption by free protons in the early ejecta that is subject to an intense neutrino flux. As a consequence, the *rp*-process takes place, which leads to the production of proton-rich nuclei beyond the iron group. In particular, the production of some light *p*-

nuclei by this neutrino-induced *rp*-process, or “ $\nu p$ -process”, is anticipated in Fröhlich et al. (2006b) and Pruet et al. (2006). In their works, however, only a small number of thermodynamic trajectories were considered for the nucleosynthesis calculations, which were also limited for the very early ejecta ( $\lesssim 1$  s after core bounce). This is due to the limitations of the hydrodynamic calculations with accurate neutrino transport currently available, which led to “successful” supernova explosions. It is obvious, however, that more investigations for various physical conditions are needed for a profound understanding of the overall picture of this newly discovered nucleosynthesis process.

In this paper, therefore, the neutrino-induced *rp*-process of nucleosynthesis in neutrino-driven winds is investigated in some detail, for various physical conditions obtained from (much simpler) semi-analytic calculations. A special attention is paid for the production of light *p*-nuclei including  $^{92,94}\text{Mo}$  and  $^{96,98}\text{Ru}$ , which cannot be explained even by the most successful scenario (i.e., the O/Ne layers in core-collapse supernovae, Prantzos et al. 1990; Rayet et al. 1995). The production of some light *p*-nuclei ( $^{74}\text{Se}$ ,  $^{78}\text{Kr}$ ,  $^{84}\text{Sr}$ , and  $^{92}\text{Mo}$ ) in slightly neutron-rich winds has also been suggested by Hoffman et al. (1996). Hence, the nucleosynthesis calculations are performed for the wide range of initial electron fractions ( $Y_e$ ) covering *both* proton-rich and neutron-rich winds. This is of particular importance to discuss whether the neutrino-driven winds can be the major production site of these light *p*-nuclei.

The thermodynamic and hydrodynamic trajectories of the neutrino-heated ejecta are obtained with the semi-analytic models of neutrino-driven winds (§ 2), which were originally developed for the study of *r*-process (Wanajo et al. 2001). This study is thus a natural extension of the previous nucleosynthesis study in Wanajo et al. (2001), to take the variation of  $Y_e$  into consideration (see also Wanajo et al. 2002; Wanajo & Ishimaru 2006b). The masses of proto-neutron stars are taken to be  $1.4 M_\odot$  and  $2.0 M_\odot$  as in Wanajo et al. (2001). The latter is regarded as the test case for (reasonably) high entropy winds (about a factor of two), which has been proposed as a possible model for the production of heavy *r*-nuclei (Otsuki et al. 2000; Wanajo et al. 2001). The nucleosynthesis in each wind trajectory is cal-

culated for the wide range of  $Y_e$  including *both* proton-rich and neutron-rich compositions (§ 3). The mass-averaged yields over the various neutrino luminosities for a given initial  $Y_e$  are compared with the solar abundances (§ 4). These results are further averaged over the  $Y_e$  distribution of the neutrino-heated ejecta obtained from the recent two-dimensional hydrodynamic calculation by Buras et al. (2006). These mass- $Y_e$ -averaged yields are compared to the solar compositions to discuss the contribution of the nucleosynthesis in neutrino-driven winds to the Galactic chemical evolution. Summary and conclusions of the current study are presented in § 5.

## 2. Neutrino-driven Wind Models

After several 100 ms from the core bounce, hot convective bubbles are evacuated from the surface of a proto-neutron star, and the winds driven by neutrino heating emerge, as can be seen in some hydrodynamic simulations of “successful” supernova explosions (Woosley et al. 1994; Buras et al. 2006). During this wind phase, a steady flow approximation may be justified. The wind trajectories in this paper are thus obtained using the semi-analytic models of neutrino-driven winds in Otsuki et al. (2000) and Wanajo et al. (2001, 2002), which were developed for the study of  $r$ -process (see also Qian & Woosley 1996; Cardall & Fuller 1997; Thompson, Burrows, & Meyer 2001). Here the models and some modifications added to them are briefly described.

In this study, a couple of hydrodynamic studies of “exploding” core-collapse supernovae are closely referred, in order to link the current parametrized models to more realistic ones. One is the one-dimensional core-collapse simulation of a  $20 M_\odot$  progenitor star in Woosley et al. (1994). This is in fact only the case that followed the wind phase for long duration (up to  $\sim 20$  s), which is relevant for the current study. It is cautioned, however, that the neutrino transport was treated rather approximately, which makes it difficult to obtain the reliable time evolution of  $Y_e$  in the neutrino-processed material. Note also that the spatial  $Y_e$  distribution cannot be obtained with one-dimensional simulations. The other is the two dimensional simulation of a collapsing  $15 M_\odot$  progenitor by Buras et al. (2006), which is also taken in Pruet et al.

(2005, 2006). The simulation was limited to the first  $\sim 0.5$  s after core bounce (and linked to a one-dimensional simulation up to  $\sim 1.3$  s), but the accurate neutrino transport was taken into account. Therefore, the obtained time variation of  $Y_e$  and its spatial distribution may be reliable.

The system is treated as time stationary and spherically symmetric, and the radius of the neutron star is assumed to be the same as that of the neutrino sphere. The physical variables in the wind are then expressed as functions of the distance  $r$  from the center of the neutron star. The ejected mass by neutrino heating is assumed to be negligible compared to the mass of the neutron star. Therefore, the gravitational field in which the neutrino-heated matter moves can be treated as a fixed-background Schwarzschild metric. The velocity  $v(r)$ , temperature  $T(r)$ , and density  $\rho(r)$  can be solved with their boundary conditions by use of relations based on baryon, momentum, and energy conservation (eqs. (1)-(3) in Wanajo et al. 2001). The source term in the equation of energy conservation is due to both heating and cooling by neutrino interactions. The gravitational redshift of the neutrino energies, and the bending of the neutrino trajectories expected from general relativistic effects, are explicitly taken into account (Otsuki et al. 2000). The neutrino luminosities  $L_\nu$  of all neutrino flavors are assumed to be equal, and the rms average neutrino energies are taken to be 10, 20, and 30 MeV, for electron, anti-electron, and the other flavors of neutrinos, respectively.

As the boundary conditions at the neutrino sphere, the density is taken to be  $10^{10} \text{ g cm}^{-3}$  and the temperature is determined so that heating and cooling by neutrino interactions are in equilibrium. The mass ejection rate at the neutrino sphere  $\dot{M}$  that determines the initial velocity is set to be  $\dot{M} = 0.99 \times \dot{M}_c$ . Here  $\dot{M}_c$  is the critical value that gives the transonic solution. The wind with  $\dot{M}_c$  becomes supersonic through the sonic point, while those with  $\dot{M} < \dot{M}_c$  are subsonic throughout. In fact, recent hydrodynamic simulations show that the fast wind collides with the dense shell of slower ejecta behind the shock and is decelerated again to be subsonic (e.g., Buras et al. 2006). On the other hand, the subsonic wind, which cannot escape by itself from the gravitational potential, must be enough fast (i.e.,  $\dot{M} \approx \dot{M}_c$ ) to reach the early *bubble* ejecta. For example, the wind is too slow

to reach the ejecta behind the shock (at several 1000 km) when  $\dot{M}$  is taken to be, e.g.,  $0.9 \times \dot{M}_c$ . Thus, the choice of  $\dot{M}$  above may be reasonable.

In this study, the neutron star masses  $M$  are taken to be  $1.4 M_\odot$  and  $2.0 M_\odot$ . The radius of neutrino sphere is assumed to be  $R_\nu(L_\nu) = (R_{\nu 0} - R_{\nu 1})(L_\nu/L_{\nu 0}) + R_{\nu 1}$  as a function of  $L_\nu$ , where  $R_{\nu 0} = 30$  km,  $R_{\nu 1} = 10$  km, and  $L_{\nu 0} = 4 \times 10^{52}$  ergs s $^{-1}$ , as shown in Figure 1 (*dashed line*). This mimics the early time evolution of neutrino sphere that can be seen in realistic core-collapse simulations (Woosley et al. 1994; Buras et al. 2006, see also Figures 2 and 3). In Figure 1,  $\dot{M}$  for each  $M$  is also shown as a function of  $L_\nu$  (*solid line*). The resulted (asymptotic) entropy per baryon  $s$  and the dynamic timescale  $\tau_{\text{dyn}} (\equiv |\rho/(d\rho/dt)|_{T=0.5 \text{ MeV}})$  are denoted by thick solid and dot dashed lines, respectively. As can be seen, the model of  $M = 2.0 M_\odot$  results in higher  $s$ , shorter  $\tau_{\text{dyn}}$ , and smaller  $\dot{M}$ . In particular, the entropy is about as twice as that for the  $M = 1.4 M_\odot$  model all the way, which might lead to the production of the heavy  $r$ -process nuclei (Otsuki et al. 2000; Wanajo et al. 2001).

It should be noted that no hydrodynamic studies to date indicate the formation of such a massive proto-neutron star (with the radius of  $\sim 10$  km). On the other hand, a recent hydrodynamic simulation shows an entropy increase owing to the collision with the slower preceding ejecta, resulting  $s \sim 80 N_A k$  at early times ( $\sim 1$  s, Pruet et al. 2005; Buras et al. 2006). Furthermore, some other mechanisms that increase entropy have been also proposed (e.g., Qian & Woosley 1996; Thompson 2003; Suzuki & Nagataki 2005; Burrows et al. 2006). In fact, when it comes to merely entropy, the model of  $M = 2.0 M_\odot$  is rather close to the hydrodynamic implication in Pruet et al. (2005) as far as during the early epoch. Thus, this model can be regarded simply as a *reasonably* high entropy case that would be expected in realistic simulations, rather than an extreme case with a very massive proto-neutron star. This may be better than to obtain the higher entropy by multiplying a certain factor to the density or temperature with no physical basis. It should be stressed that the time variations of  $T$ ,  $\rho$ , and  $r$  are obtained consistently in the current study, which are all important for the nucleosynthesis (§ 3.3).

The wind trajectories are calculated for 54 con-

stant  $L_\nu$  of  $40 - 0.5 \times 10^{51}$  ergs s $^{-1}$  with the intervals of  $1 \times 10^{51}$  ergs s $^{-1}$  and  $1 \times 10^{50}$  ergs s $^{-1}$  for  $L_\nu \geq 2 \times 10^{51}$  ergs s $^{-1}$  and  $L_\nu < 2 \times 10^{51}$  ergs s $^{-1}$ , respectively. The set of time stationary solutions  $v(r)$ ,  $T(r)$ , and  $\rho(r)$  are then converted to the time variables  $r(t)$ ,  $T(t)$ , and  $\rho(t)$  for the nucleosynthesis calculations, where  $t$  is the time that is set to zero at the neutrino sphere for a given wind.

In order to link the series of constant  $L_\nu$  trajectories to realistic time-evolving winds, the post bounce time for each  $L_\nu$  is defined as  $t_{\text{pb}}(L_\nu) = t_0 (L_\nu/L_{\nu 0})^{-1}$ , where  $t_0 = 0.2$  s (Figure 1, *dotted line*). This is needed to determine the ejected mass by each wind (i.e.,  $\dot{M}(L_\nu) \Delta t_{\text{pb}}$ ) when calculating the mass-averaged nucleosynthesis yields (§ 4). This gives  $L_\nu(t_{\text{pb}}) = L_{\nu 0}(t_{\text{pb}}/t_0)^{-1}$  and  $R_\nu(t_{\text{pb}}) = (R_{\nu 0} - R_{\nu 1})(t_{\text{pb}}/t_0)^{-1} + R_{\nu 1}$  (Figs. 2 and 3), which approximately mimic the hydrodynamic results in Woosley et al. (1994).

The time evolutions of  $r$ ,  $T_9$  ( $\equiv T/10^9$  K),  $\rho$ , and  $s$  (specific entropy) for selected (odd-numbered) trajectories are shown in Figures 2 (for  $M = 1.4 M_\odot$ ) and 3 (for  $M = 2.0 M_\odot$ ). In these figures, the time is set to  $t = 0$  at  $t_{\text{pb}} = t_{\text{pb}}(L_\nu)$  for each wind. As can be seen in the top panels of these figures, the time evolutions of radii for  $t_{\text{pb}} > 0.5$  s are very similar to those found in the hydrodynamic results (Woosley et al. 1994; Buras et al. 2006), at which the current wind solutions may be justified. On the other hand, the early time evolutions for  $t_{\text{pb}} < 0.5$  s seem less realistic, in which the convective bubbles dominate in a realistic simulation (Buras et al. 2006). This may not cause a severe problem, since the  $rp$ -process takes place dominantly at  $t_{\text{pb}} > 0.5$  s as discussed in § 3.3. Both models ( $M = 1.4 M_\odot$  and  $2.0 M_\odot$ ) show qualitatively similar thermodynamic histories as can be seen in Figures 2 and 3. Note, however, that the entropy is about a factor of two higher for the  $M = 2.0 M_\odot$  model all the way.

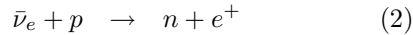
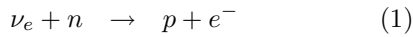
### 3. Nucleosynthesis in Winds

#### 3.1. Reaction Network

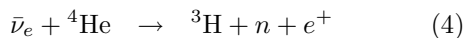
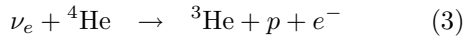
Adopting the wind trajectories discussed in § 2 for the physical conditions, the nucleosynthetic yields are obtained by solving an extensive nuclear reaction network code. The network consists of 6300 species between the proton and neutron drip lines predicted by a recent fully micro-

scopic mass formula (HFB-9, Goriely et al. 2005), all the way from single neutrons and protons up to the  $Z = 110$  isotopes. All relevant reactions, i.e.  $(n, \gamma)$ ,  $(p, \gamma)$ ,  $(\alpha, \gamma)$ ,  $(p, n)$ ,  $(\alpha, n)$ ,  $(\alpha, p)$ , and their inverse are included. The experimental data whenever available and the theoretical predictions for light nuclei ( $Z < 10$ ) are taken from the REA-CLIB compilation (F. -K. Thielemann 1995, private communication). All other reaction rates are taken from the Hauser-Feshbach rates of BRUS-LUB (Aikawa et al. 2005) making use of experimental masses (Audi, Wapstra, & Thibault 2003) whenever available or the HFB-9 mass predictions (Goriely et al. 2005) otherwise. The photodisintegration rates are deduced applying the reciprocity theorem with the nuclear masses considered. The  $\beta$ -decay rates are taken from the gross theory predictions (GT2, Tachibana, Yamada, & Yoshida 1990), obtained with the HFB-9  $Q_\beta$  predictions (T. Tachibana 2005, private communication). Electron capture reactions on free nucleons as well as on heavy nuclei are also included (Fuller, Fowler, & Newman 1982; Langanke & Martinez-Pinedo 2001).

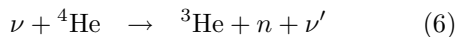
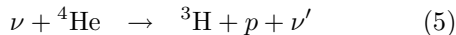
Rates for neutrino capture on free nucleons



and  $^4\text{He}$ ,



as well as for neutrino spallation of free nucleons from  $^4\text{He}$ ,



are also included (Woosley et al. 1990; McLaughlin, Fuller, & Wilson 1996). Neutrino-induced reactions of heavy nuclei are not included in this study, which may have only minor effects (Meyer, McLaughlin, & Fuller 1998). The rates for neutrino reactions above are expressed as (Qian et al. 1997)

$$\lambda_\nu \approx 4.97 \left( \frac{L_\nu}{10^{51} \text{ ergs s}^{-1}} \right) \left( \frac{\text{MeV}}{\langle E_\nu \rangle} \right) \times \left( \frac{100 \text{ km}}{r} \right)^2 \left( \frac{\langle \sigma_\nu \rangle}{10^{-41} \text{ cm}^2} \right) \text{ s}^{-1}, \quad (7)$$

where  $\langle E_\nu \rangle$  and  $\langle \sigma_\nu \rangle$  are the average energy and cross section of the neutrino species responsible for the reaction. The time evolution of  $L_\nu$  (that is taken to be constant when deriving the wind trajectories) is taken into account, according to  $L_\nu(t_{\text{pb}})$  in § 2. The distance  $r$  from the center of the neutron star for each wind as a function of time can be seen in Figures 2 and 3.

### 3.2. Initial Compositions and $Y_e$

Each calculation is initiated when the temperature decreases to  $T_9 = 9$  (where  $T_9 \equiv T/10^9 \text{ K}$ ). At this high temperature, the compositions in the nuclear statistical equilibrium (NSE) are obtained (mostly free nucleons and  $\alpha$  particles) immediately after the calculation starts. The initial compositions are thus given by  $X_n = 1 - Y_{ei}$  and  $X_p = Y_{ei}$ , respectively, where  $X_n$  and  $X_p$  are the mass fractions of neutrons and protons, and  $Y_{ei}$  is the initial electron fraction (number of proton per nucleon) at  $T_9 = 9$ . In a core-collapse simulation for long duration ( $\sim 20 \text{ s}$ , Woosley et al. 1994), it is observed that the initial  $Y_e$  takes mostly a constant value ( $\approx 0.46$ ) during the early phase ( $t_{\text{pb}} = \text{a few s}$ ), and gradually decreases to  $\approx 0.38$ . This is due to the hardening of the anti-electron neutrino spectrum relative to that of the electron neutrino at later times (Qian & Woosley 1996). In order to mimic this effect,  $Y_{ei}$  is assumed to be constant ( $Y_{e0}$ ) for  $t_0 < t_{\text{pb}} \leq t_1$  and  $Y_{ei}(t_{\text{pb}}) = (Y_{e0} - Y_{e1})(t_{\text{pb}}/t_1)^{-1} + Y_{e1}$  for  $t_{\text{pb}} > t_1$ , where  $t_1 = 4 \text{ s}$  and  $Y_{e1} = 0.1$ . This gives  $Y_{ei}$  for each wind such as  $Y_{ei} = Y_{e0}$  and  $Y_{ei}(L_\nu) = (Y_{e0} - Y_{e1})(L_\nu/L_{\nu 0})(t_1/t_0) + Y_{e1}$  for  $L_\nu \geq 2 \times 10^{51} \text{ ergs s}^{-1}$  and  $L_\nu < 2 \times 10^{51} \text{ ergs s}^{-1}$ , respectively.

The core-collapse simulation in Woosley et al. (1994) shows that the neutrino-heated ejecta at the first few seconds is *neutron rich* ( $Y_e \approx 0.46$ ). On the other hand, recent hydrodynamic studies with more accurate neutrino transport show that the bulk of the ejecta during the early phase is *proton rich* ( $Y_e \gtrsim 0.5$ , Liebendörfer et al. 2003; Kitaura, Janka, & Hillebrandt 2006; Buras et al. 2006). The reason of this proton richness is that, when the degeneracy is lifted, the mass difference between the proton and neutron favors the proton-rich composition as far as the differences of luminosities and mean energies between the electron neutrinos and the anti-electron neutrinos are not

significant. As a result, the electron neutrino capture (eq. [1]) and the positron capture (inverse of eq. [2]) overcome their inverses, resulting in  $Y_e > 0.5$  (see Hoffman et al. 1996; Fröhlich et al. 2006a; Buras et al. 2006, for more detailed discussion). In this study, the nucleosynthesis calculation for each wind is repeated for various  $Y_{e0}$  ( $= 0.45-0.65$ ) with the interval of 0.005 (41 cases), covering the slightly neutron-rich to very proton-rich compositions. In Figure 4 (*top panel*), the time variations of  $Y_{ei}$  that determines the initial composition for each wind are shown for the winds of  $M = 2.0 M_\odot$  with  $Y_{e0} = 0.60$  (*thin solid line*) and  $M = 1.4 M_\odot$  with  $Y_{e0} = 0.48$  (*thin dotted line*), respectively.

Neutrino capture on free nucleons changes  $Y_e$  (“ $\alpha$  effect”, McLaughlin, Fuller, & Wilson 1996; Meyer, McLaughlin, & Fuller 1998). Figure 5 shows  $Y_e$  (*thick lines*) along with the mass fractions (*thin lines*) of neutrons  $X_n$ , protons  $X_p$ ,  $\alpha$  particles  $X_\alpha$ , and heavy nuclei  $X_h$  ( $Z > 2$ ) as functions of  $T_9$ , obtained from nucleosynthesis calculations for the winds with  $M = 2.0 M_\odot$ ,  $L_\nu = 1 \times 10^{52}$  ergs s $^{-1}$ , and  $Y_{e0} = 0.60$  (W201060, *solid lines*) and  $M = 1.4 M_\odot$ ,  $L_\nu = 1 \times 10^{52}$  ergs s $^{-1}$ , and  $Y_{e0} = 0.48$  (W141048, *dotted lines*), respectively<sup>1</sup>. For the wind W201060,  $Y_e$  decreases significantly as the temperature drops. This is due to the increasing  $\alpha$  particles, which continues as far as neutrons are supplied from the neutrino capture on protons (eq. [2]). The electron fraction can be expressed as

$$Y_e \approx X_p + \frac{X_\alpha}{2} + \sum_{Z>2,A} Z Y(Z, A), \quad (8)$$

where  $Y(Z, A)$  is the abundance (number fraction per nucleon, i.e., the mass fraction divided by  $A$ ) of the nucleus ( $Z, A$ ). For W201060, alpha particles dominate with a small fraction of protons as soon as the temperature drops to  $T_9 \sim 7$ . Hence the second term of equation (8) governs  $Y_e$ , while the third term is negligible. As a result,  $Y_e$  decreases toward 0.5. Note that the decrease of  $Y_e$  for  $T_9 \lesssim 3$  is due to the ( $n, p$ ) reactions during the  $rp$ -process phase and the  $\beta^+$ -decays after freezeout (§ 3.3). On the other hand, for W141048,  $\alpha$  particles and

also heavy nuclei dominate at  $T_9 \sim 6$ . Thus,  $Y_e$  is determined by the second and third terms in equation (8). The sum of these two terms are close to the original  $Y_e$  value ( $= 0.48$ ), owing to the slight neutron richness of heavy nuclei. As a result,  $Y_e$  keeps its original value.

This can be seen in Figure 4 (*bottom panel*), in which the changes of  $Y_e$ ,  $\Delta Y_e$ , until the temperature drops to  $T_9 = 3$  (at which the  $rp$ -process begins, see § 3.3) as function of  $Y_{e0}$ , for the winds with  $M = 1.4 M_\odot$  (*dotted line*) and  $2.0 M_\odot$  (*solid line*). The change is not significant for  $Y_{e0} \approx 0.47 - 0.48$  as described above. For a larger  $Y_{e0}$  case ( $> 0.5$ ),  $|\Delta Y_e|$  is greater for the more massive  $M$  ( $= 2.0 M_\odot$ ) model at later times ( $t_{pb} = 4$ , i.e.,  $L_\nu = 2 \times 10^{51}$  ergs s $^{-1}$ ). This is due to the greater entropy for these winds (see Figures 1-3) that leave more free protons for  $Y_e > 0.5$ . For the same reason,  $|\Delta Y_e|$  is also greater for a larger  $Y_{e0}$  case. For a smaller  $Y_{e0}$  case ( $\lesssim 0.47$ ),  $\Delta Y_e$  takes a positive value owing to the abundant neutrons. The electron fraction at  $T_9 = 3$ , defined as  $Y_{ef} \equiv Y_{ei} + \Delta Y_e$ , is shown as a function of  $t_{pb}$  in Figure 4 (*top panel*, *thick lines*) for the winds of  $M = 2.0 M_\odot$  with  $Y_{e0} = 0.60$  (*solid line*) and  $M = 1.4 M_\odot$  with  $Y_{e0} = 0.48$  (*dotted line*). At later times ( $t_{pb} > 4$  s), in which the material is assumed to be rather neutron rich,  $Y_e$  increases significantly owing to the neutrino effect and takes  $\approx 0.34-0.36$  at  $t_{pb} = 16$  s ( $L_\nu = 5 \times 10^{50}$  ergs s $^{-1}$ ). Note that the time evolution of  $Y_{ef}$  for  $M = 1.4 M_\odot$  with  $Y_{e0} = 0.48$  (Fig. 4, *top panel*, *thick dotted line*) is similar to the hydrodynamic result in Woosley et al. (1994).

### 3.3. The $rp$ -Process in Proton-rich Winds

In the proton-rich compositions with the presence of intense neutrino flux, the proton capture proceeds beyond the iron group nuclei by bypassing the  $\beta^+$ -waiting point nuclei, as shown in recent works (Fröhlich et al. 2006b,a; Pruet et al. 2005; Wanajo 2006). This can be clearly seen in Figure 6, which compares the snapshots of nucleosynthesis at  $t = 0.22$  s $^2$  (when the temperature drops to  $T_9 \approx 2$ ) for W141060 without (*left panel*) and with (*right panel*) neutrino reactions. Without neutrino reactions, the nuclear flow cannot advance beyond  $^{64}\text{Ge}$ , whose  $\beta^+$  half life is

<sup>1</sup>The wind trajectory with  $M = i.j M_\odot$ ,  $L_\nu = kl \times 10^{51}$  ergs s $^{-1}$ , and  $Y_{e0} = 0.mn$  is labeled as  $Wijklmn$ , hereafter.

<sup>2</sup>In this section, the time is set to  $t = 0$  at  $T_9 = 9$ .

1.06 minutes<sup>3</sup>. In contrast, the neutrino capture on abundant protons (eq. [2]) provides a fraction of neutrons that immediately suffer  $(n, p)$  reactions. Note that the  $(n, p)$  reaction acts as the same as the  $\beta^+$ -decay of a given species. As a result, the nuclear flow proceeds to the heavier proton-rich species (Fig. 6, *right panel*).

It is interesting to note that the proton-to-seed abundance ratio  $Y_p/Y_h$  at this point (Figure 6, *right panel*) is still high ( $= 49$ ) despite the moderate entropy ( $55 N_A k$ ). This is due to the slowness of the  $\alpha + \alpha + \alpha \rightarrow {}^{12}\text{C}$  reaction that is the bottleneck for the production of heavy nuclei. This is in contrast to the neutron-rich compositions, in which the faster  $\alpha + \alpha + n \rightarrow {}^9\text{Be}$  reaction followed by  $\alpha$  capture is efficient. This is why the entropy of a few  $100 N_A k$  is needed for the  $r$ -process in neutrino-driven winds (Woosley et al. 1994; Wanajo et al. 2001). In the proton-rich compositions, however, only a moderate entropy is sufficient for the occurrence of  $rp$ -process.

This *neutrino-induced*  $rp$ -process can be seen more clearly for the wind models with  $M = 2.0 M_\odot$ . This is a consequence of their higher entropies (see Figures 1-3), which leave more protons needed for the  $rp$ -process. Figure 7 shows the snapshots of nucleosynthesis calculations for the winds W201060 (*top panels*), W200865 (*middle panels*), and W200265 (*bottom panels*) during ( $T_9 \approx 2$ , *left panels*) and after ( $t \approx 1.0$  s, *right panels*) the  $rp$ -process phase. For the same  $L_\nu$  and  $Y_{e0}$  to W141060 (Fig. 6, *right panel*) but with  $M = 2.0 M_\odot$  (W201060),  $Y_p/Y_h$  is three times greater ( $= 151$ ) at  $T_9 = 2$  (Fig. 7, *top left*), owing to its higher entropy ( $= 92 N_A k$ ). As a result, the nuclear flow proceeds to the  $Z = 50$  magic nuclei, which leads to the production of the  $p$ -nuclei with  $A \sim 110$ .

The detailed nuclear flow patterns for W201060 when the  $rp$ -process is active ( $T_9 = 2.5$ ) are shown in Figure 8. Here, the nuclear flow for each reac-

tion  $i \rightarrow j$  is defined as

$$F_{ij} \equiv \dot{Y}(i \rightarrow j) - \dot{Y}(j \rightarrow i) \quad \text{s}^{-1}. \quad (9)$$

In Figure 8,  $F_{ij}$  and  $Y_i$  (for those greater than  $10^{-5}$ ) are shown in logarithmic scale by arrows and circles, respectively. As can be seen,  $(p, n)$  reactions play a dominant role to carry away the nuclear abundances from waiting points, while the contribution of  $\beta^+$ -decays (off-centered arrows) is minor.

The time variations of the mass fractions (*thin lines*) of neutrons  $X_n$ , protons  $X_p$ ,  $\alpha$  particles  $X_\alpha$ , and heavy nuclei  $X_h$  for W201060 are shown in Figure 9, along with those of the average mass number of heavy nuclei  $A_h$  and the temperature (*thick lines*), where

$$X_h \equiv \sum_{Z>2, A} X(Z, A) \quad (10)$$

and

$$A_h \equiv \frac{1}{X_h} \sum_{Z>2, A} A X(Z, A). \quad (11)$$

The results with all neutrino-induced reactions (eqs. [1]-[6]), neutrino capture on free nucleons only (eqs. [1] and [2]), and no neutrino-induced reactions are denoted by the solid, dashed, and dotted lines, respectively. The initiation of the  $rp$ -process can be clearly seen as the sudden increase of  $A_h$  at  $T_9 \approx 3$ , for the cases with neutrino reactions (*thick solid* and *thick dashed lines*). This is due to the presence of neutrons ( $X_n \sim 10^{-11}$ ) by the neutrino capture on abundant protons (eq. [2]), as can be seen in Figure 9 (*thin solid* and *thin dashed lines*).

The neutrino reactions for  ${}^4\text{He}$  tend to inhibit the  $rp$ -process as can be seen in Figure 9, although their effects are moderate. This is due to the spallation reactions of  ${}^4\text{He}$  (eqs. [5] and [6]), while the capture reactions (eqs. [3] and [4]) are not important (because of their smaller cross sections). The resulting  ${}^3\text{H}$  emitted from the neutrino spallation of equation (5) immediately suffers a  $(p, n)$  reaction to  ${}^3\text{He}$  in the proton-rich compositions. These  ${}^3\text{He}$  nuclei, in addition to those from the spallation reaction of equation (6), capture abundant  $\alpha$  particles to be  ${}^7\text{Be}$ , which further capture  $\alpha$  particles. As a result, a fraction of  ${}^4\text{He}$  assembles into heavier nuclei that act as “neutron poison”, resulting in the smaller neutron abundance (Figure 9). This is

<sup>3</sup>In the current reaction network,  ${}^{65}\text{As}$  is omitted, whose proton separation energy is predicted to be negative in the HFB-9 mass formula (Goriely et al. 2005). In principle, the nuclear flow can proceed through  ${}^{65}\text{As}$  by two proton capture reaction even with the (small) negative proton separation energy, owing to the presence of the Coulomb barrier. Inclusion of this isotope would not change the current result, however, since the time scale of this two  $p$  reaction is no less than  $\sim 1$  s (Brown et al. 2002).

a similar mechanism shown by Meyer (1995), i.e., the  $r$ -process is also inhibited by these neutrino reactions on  ${}^4\text{He}$  in the neutron-rich compositions. It should be noted that the relatively large mean energies of  $\mu$  and  $\tau$  neutrinos assumed in this study (according to Woosley et al. (1994)) may lead to the overestimation of this effect.

In order to see the gross feature of the neutrino-induced  $rp$ -process more clearly, the time variations of the mean lifetimes for  $\beta^+$ -decay,  $(n, \gamma)$ ,  $(p, \gamma)$ , and  $(n, p)$  reactions, and neutrino capture on protons (eq. [2]) are shown in Figure 10 (*solid lines*), where

$$\tau_{\beta^+} \equiv \left[ \frac{1}{Y_h} \sum_{Z>2, A} \lambda_{\beta^+}(Z, A) Y(Z, A) \right]^{-1}, \quad (12)$$

$$\tau_{n\gamma} \equiv \left[ \frac{\rho Y_n}{Y_h} \sum_{Z>2, A} \lambda_{n\gamma}(Z, A) Y(Z, A) \right]^{-1}, \quad (13)$$

$$\tau_{p\gamma} \equiv \left[ \frac{\rho Y_p}{Y_h} \sum_{Z>2, A} \lambda_{p\gamma}(Z, A) Y(Z, A) \right]^{-1}, \quad (14)$$

$$\tau_{np} \equiv \left[ \frac{\rho Y_n}{Y_h} \sum_{Z>2, A} \lambda_{np}(Z, A) Y(Z, A) \right]^{-1}, \quad (15)$$

and

$$\tau_{\bar{\nu}_e p} \equiv \lambda_{\bar{\nu}_e p}^{-1}. \quad (16)$$

Here,

$$Y_h \equiv \sum_{Z>2, A} Y(Z, A) \quad (17)$$

and  $\lambda_{\beta^+}(Z, A)$ ,  $\lambda_{n\gamma}(Z, A)$ ,  $\lambda_{p\gamma}(Z, A)$ ,  $\lambda_{np}(Z, A)$ , and  $\lambda_{\bar{\nu}_e p}$  are the rates of the corresponding reactions. The rates in equations (12)-(15) are averaged over the heavy nuclei, which represent the lifetimes of the dominant isotopes at a given time. The dotted lines are the corresponding lifetimes when the sum in equations (12)-(15) are taken for  $Z \geq 48$  only. With the timescales defined above, the requisite condition for the neutrino-induced  $rp$ -process can be expressed as

$$\tau_{p\gamma} \ll \tau_{np} \ll \tau_{\beta^+}. \quad (18)$$

Note that the conditions for the  $r$ -process and classical  $rp$ -process are simply  $\tau_{n\gamma} \ll \tau_{\beta^+}$  and  $\tau_{p\gamma} \ll \tau_{\beta^+}$ , respectively.

Top panel of Figure 10 is the result for the wind trajectory of W201060 that is taken to be the reference case here. As can be seen, the  $(n, p)$  reactions are faster than the  $\beta^+$ -decays all the way during the first one second. This shows clearly the importance of the  $(n, p)$  reactions for the neutrino-induced  $rp$ -process. The role of  $(n, \gamma)$  reactions is minor, compared to  $(n, p)$  reactions. A saturation of  $A_h$  at  $t =$  a few 100 ms ( $T_9 \sim 2$ ) in Figure 9 indicates the termination of the neutrino-induced  $rp$ -process. At later times,  $A_h$  slightly decreases by photodisintegration. Note that this termination is *not* due to the exhaustion of protons, as in the case of  $r$ -process that ceases generally by the neutron exhaustion (Wanajo et al. 2004). The proton-to-seed abundance ratio is still high at later times (e.g.,  $Y_p/Y_h = 77$  at  $t = 1$  s), and the bulk of  $(p, \gamma)$  reactions are enough fast throughout (Fig. 10, *solid line*). However, the  $(p, \gamma)$  reactions for the heaviest nuclei ( $Z \geq 48$ ; Fig. 10, *dotted line*) become slow owing to the increasing Coulomb barrier, and compete with the  $(n, p)$  reactions (i.e.,  $\tau_{p\gamma} \sim \tau_{np}$ ) at  $t \sim 0.1$  s ( $T_9 \sim 2$ ). This results in the broadening and smoothing of the abundances for  $Z > 40$  in Figure 7 (*top panels*), which is similar to the “freezeout effect” seen in the  $r$ -process (Wanajo et al. 2004).

What terminates the  $rp$ -process is thus the Coulomb barrier of the heaviest nuclei in the nuclear flow, which breaks the relation between the first two in equation (18). The slowness of the  $(n, p)$  reactions that compete with the  $\beta^+$ -decays ( $\tau_{np} \sim \tau_{\beta^+}$ ) can be another reason to cease the  $rp$ -process. The  $(n, p)$  reactions becomes significantly slow owing to the less active neutrino capture on protons (Figure 10) at later times ( $t \gtrsim 1$  s), whose lifetime is proportional to the square of  $r$  (eqs. [7] and [16]). For the current wind trajectory (W201060), the relation between the latter two in equation (18) breaks only at late times ( $t \approx 1$  s for  $Z \geq 2$  and  $t \approx 7$  s for  $Z \geq 48$ ). This shows that the supply of neutrons by the neutrino capture on protons is sufficient throughout the  $rp$ -process phase.

One may consider that the neutrino-induced  $rp$ -process proceeds to much higher atomic number to produce *all* the  $p$ -nuclei up to  $A \sim 200$ , *if* the proton concentration is much higher owing to, e.g., a larger  $Y_{e0}$  or a higher entropy. This may not be true, however, as can be seen in Fig-



ure 7. For the wind trajectory with a larger entropy ( $= 103 N_A k$ ) and  $Y_{e0} (= 0.65, \text{W200865})$  that results in  $Y_{ef} = 0.582$ ,  $Y_p/Y_h = 427$  at  $T_9 = 2$  and the nuclear flow proceeds beyond  $Z = 50$  (Figure 7, *middle panels*). In fact, this wind results in the production of the heaviest  $p$ -nuclei ( $A \sim 130$ ) in the current study. However, the flow deviates from the proton-drip line and reaches the  $\beta$ -stability line (Figure 7, *middle right*, see also Pruet et al. 2006). This is *not* due to the  $\beta^+$ -decays of the heaviest nuclei, which are rather slow all the way ( $\tau_{\beta^+} \sim 100$  s for  $Z \geq 48$ ; Fig. 10, *middle panel*, *dotted line*). This is a consequence of the slowness of proton capture owing to the higher and higher Coulomb barrier for the heaviest nuclei in the flow, which competes with both  $(n, p)$  and  $(n, \gamma)$  reactions as can be seen in Figure 10 (*middle panel*, *dotted lines*). It should be also noted that there are  $\alpha$  unbound nuclei  $^{106-108}\text{Te}$  ( $Z = 52$ ), which is regarded as the end point of the *classical*  $rp$ -process (Schatz et al. 2001). In addition, the proton capture also slows substantially when the temperature drops below  $T_9 \sim 2$  (Figure 10). Thus, the temperature range in which the neutrino-induced  $rp$ -process takes place is strictly limited to  $2 \lesssim T_9 \lesssim 3$ . This differs significantly from the neutron capture without Coulomb barrier in case of the  $r$ -process.

At the later wind phase, the entropy increases significantly, as can be seen in Figures 1-3. The situation is even worse (but interesting), however, for the production of proton-rich nuclei. The snapshots of the nucleosynthesis calculations for the wind trajectory of W200265 is shown in Figure 7 (*bottom panels*). This wind obtains the highest entropy ( $= 176 N_A k$ ) during the proton-rich phase assumed in this study ( $t_{\text{pb}} \leq 4$  s, see Fig. 4, *top panel*). As can be seen, the nuclear flow cannot sustain its proton richness and runs toward the  $\beta$ -stability when the temperature drops to  $T_9 \approx 2$  (Figure 7, *bottom left*) despite its extremely high  $Y_p/Y_h (= 858)$ . At later times, the  $(n, \gamma)$  reactions push the flow to the neutron-rich side (Figure 7, *bottom right*). The reason is that the temperature falls off to  $T_9 \approx 1$  quickly in the later winds (Figure 3). In addition, high  $Y_p/Y_h$  also results in (moderately) high  $Y_n/Y_h$  with the presence of intense neutrino flux. As shown in Figure 10 (*bottom panel*), when the temperature is below  $T_9 \sim 2$ , the  $(p, \gamma)$  reactions for the heaviest nuclei in the

flow become significantly slow, while the  $(n, \gamma)$  reactions are still active. As can be seen in these examples, the neutrino-induced  $rp$ -process may not lead to the significant production of  $p$ -nuclei beyond  $A \sim 130$ . It is interesting to note that many of the nuclei synthesized here (Fig. 7, *bottom right panel*) are usually assigned as  $s$ -nuclei or even  $r$ -nuclei, which are now synthesized in *proton-rich* compositions (see also Pruet et al. 2006).

### 3.4. $^{92}\text{Mo}$ Production in Slightly Neutron-rich Winds

In slightly neutron-rich compositions ( $Y_e \approx 0.47 - 0.49$ ), two dominant quasi-statistical-equilibrium (QSE) clusters are formed around  $A \approx 60$  and  $A \approx 90$  during the  $\alpha$ -process phase ( $T_9 \approx 7 - 4$ ). At the end of the  $\alpha$ -process phase, the matter consists of mostly  $\alpha$  particles, the heavy nuclei belong to these two QSE clusters, and a fraction of free nucleons (Figure 12). As soon as the  $\alpha$ -process ceases, the proton capture plays an important role for the production of the  $p$ -isotope  $^{92}\text{Mo}$  as suggested by Hoffman et al. (1996), whose origin has been a long-standing mystery (see Arnould & Goriely 2003, for a recent review). The nucleosynthesis calculations covering the slightly neutron-rich winds are thus needed to estimate their possible contribution to the Galactic chemical evolution of the light  $p$ -nuclei.

As shown in Figure 11, a fraction of the most dominant species  $^{90}\text{Zr}$  ( $N = 50, Z = 40$ ) in the QSE cluster (at  $A \sim 90$ ) flows into  $^{92}\text{Mo}$  ( $N = 50, Z = 42$ ) through various nuclear reaction channels. The abundance of  $^{92}\text{Mo}$  reaches 17% of its final value at this time ( $T_9 = 3.5$ ). Here, the  $(p, n)$  reaction plays a dominant role to carry away the nuclear abundances from  $^{90}\text{Zr}$ . In Figure 12, the time variations of the mass fractions (*thin lines*) of neutrons  $X_n$ , protons  $X_p$ ,  $\alpha$  particles  $X_\alpha$ , heavy nuclei  $X_h$ ,  $^{90}\text{Zr}$ , and  $^{92}\text{Mo}$  for the wind trajectory of W141048 are shown, along with those of the average mass number of heavy nuclei ( $A_h$ , eq. [11]) and the temperature (*thick lines*). Note that the neutrino effect on  $Y_e$  is negligible for this wind as described in § 3.1, i.e.,  $Y_{ef} \approx Y_{e0} = 0.48$ . The decrease of  $X_p$  slows as the QSE cluster that contains  $^{90}\text{Zr}$  grows (at  $T_9 \approx 5$ ), in order to balance with the electron fraction of the cluster ( $\approx 0.44$ ) that is smaller than that of the wind material ( $\approx 0.48$ ). These protons are gradually absorbed by the nu-

clei in this cluster after the  $\alpha$ -process phase. As a result, the abundance of  $^{92}\text{Mo}$  increases, reaching its half final value at  $T_9 = 3.2$ .

The enhancement of  $^{92}\text{Mo}$  in this way is highly dependent on the temperature history of the wind after the  $\alpha$ -process phase. The production of  $^{92}\text{Mo}$  relies largely upon the slower  $(p, n)$  reactions (mean lifetime of about 30 ms at  $T_9 = 3.5$ ) on  $^{90}\text{Zr}$ , since the photodisintegration impedes the much faster  $(p, \gamma)$  reaction at this time (Figure 11). Another channel, that is the  $(n, \gamma)$  reaction on  $^{90}\text{Zr}$ , also contributes but suffers from its inverse. The  $(p, \gamma)$  reaction on  $^{90}\text{Zr}$  becomes effective only when the temperature drops below  $T_9 \approx 2.7$  for W141048. Therefore, a relatively long cooling timescale of the wind material is required to obtain a large abundance of  $^{92}\text{Mo}$  (that is close to its QSE value, see Hoffman et al. 1996). In the current study, the subsonic solutions of winds with  $\dot{M} \approx \dot{M}_c$  are adopted as discussed in § 2. As a result, the wind is decelerated when passing over the sonic radius, and thus the decrease of temperature slows down. For the early winds ( $t_{\text{pb}} < 1$  s), this transition takes place around  $T_9 \approx 4 - 3$ . As a result,  $^{90}\text{Zr}$  suffers  $(p, n)$  and  $(n, \gamma)$  reactions for longer duration, resulting in the more production of  $^{92}\text{Mo}$ . Other light  $p$ -nuclei, e.g.,  $^{94}\text{Mo}$  and  $^{96,98}\text{Ru}$ , are not significantly produced in this process, although  $^{74}\text{Se}$  and  $^{78}\text{Kr}$  are moderately enhanced (see § 4, see also Hoffman et al. 1996).

It should be noted that the flow patterns appeared in Figure 11 would be somewhat different when another nuclear data set were adopted (see Hoffman et al. 1996). In fact, most of the relevant reactions here are taken from the theoretical (Hauser-Feshbach) predictions, although these nuclear masses are well determined by experiments (Audi, Wapstra, & Thibault 2003). Future determinations of these rates based on experiments are highly desirable.

Neutrino-induced reactions are not of importance for the production of  $^{92}\text{Mo}$  in these neutron-rich winds. The results with all neutrino-induced reactions (eqs. [1]-[6]), free nucleons only (eqs. [1] and [2]), and no neutrino-induced reactions are denoted by the solid, dashed, and dotted lines, respectively. The dashed and dotted lines cannot be distinguished, which means that the neutrino capture on free nucleons plays no role. This is due to their small abundances as can be seen in Figure 12.

The neutrino capture on  $^4\text{He}$  does not play a significant role, either. The spallation of free nucleons from  $^4\text{He}$ , on the other hand, slightly enhances the abundance of  $^{92}\text{Mo}$ . The  $^3\text{H}$  and  $^3\text{He}$  nuclei emitted from the spallation reactions (eqs. [5] and [6]) immediately capture abundant  $\alpha$  particles to be  $^7\text{Be}$  and  $^7\text{Li}$ , which further capture  $\alpha$  particles. The spalled free nucleons can survive owing to the faster  $\alpha$  capture, resulting in the slight increase of  $^{92}\text{Mo}$  as can be seen in Figure 12.

### 3.5. The $r$ -Process in Neutron-rich Winds

At later times ( $t_{\text{pb}} > 4$  s), the entropy of the winds increases more than  $100 N_A k$  (Figs. 1-3), and  $Y_{ei}$  is assumed to be neutron rich (Fig. 4, *top panel*). This may provide the suitable condition for the production of  $r$ -process nuclei (Woosley et al. 1994; Wanajo et al. 2001). As discussed in § 4, the winds with  $M = 1.4 M_\odot$  can be the origin of only the light  $r$ -process nuclei (up to  $A \sim 130$ ; Fig. 15, *top panel*). On the other hand, the heavy  $r$ -process nuclei (up to  $A \sim 190$ ) can be produced in the winds with  $M = 2.0 M_\odot$  during the late phase (Fig. 15, *bottom panel*). This is a consequence of the higher entropies (Figs. 1-3) and in part the shorter dynamic timescales (Fig. 1) of the winds, resulting in the higher neutron-to-seed abundance ratios at the beginning of  $r$ -processing ( $T_9 \sim 3$ , see Wanajo et al. 2001; Wanajo & Ishimaru 2006b, for more detail). Note that the nucleosynthetic results in the later winds do not contribute to the production of proton-rich isotopes (§ 4), since  $Y_{ei}$  is assumed to quickly drop to be rather neutron rich (Figure 4, *top panel*).

## 4. Contribution to the Galactic Chemical Evolution

### 4.1. Mass-averaged Yields as Functions of $Y_e$

In order to estimate the contribution of the neutrino-induced  $rp$ -process in neutrino-driven winds to the Galactic chemical evolution, the nucleosynthetic yields for each  $Y_{ei}$  model (41 cases) are mass-averaged over the 54 wind trajectories weighted by  $\dot{M}(L_\nu)\Delta t_{\text{pb}}$ . Figure 13 compares the averaged mass fractions  $X_{ej}$  of  $p$ -nuclei with respect to their solar values (Anders & Grevesse 1989) as functions of  $Y_{ef}$  for  $M = 1.4 M_\odot$  (*top left*) and  $2.0 M_\odot$  (*top right*) models. Here,  $Y_{ef}$ ,

which is approximately the value at the beginning of the  $rp$ -process phase (at  $T_9 = 3$ , § 3.3), is taken at  $t_{\text{pb}} = 4$  s (at  $L_\nu = 2 \times 10^{51}$  ergs s $^{-1}$ ) as representative of different  $Y_{ef}$ . The abundances of  $^{64}\text{Zn}$  and  $^{90}\text{Zr}$  are also plotted for comparison purposes. The contribution of  $p$ -nuclei produced during the later phase ( $t > 4$  s) is not important, as discussed in § 4.2. Figure 13 also shows the results for selected winds (not mass-averaged) for  $L_\nu = 8 \times 10^{51}$  ergs s $^{-1}$  ( $t_{\text{pb}} = 1$  s, *middle panels*) and  $L_\nu = 2 \times 10^{51}$  ergs s $^{-1}$  ( $t_{\text{pb}} = 4$  s, *bottom panels*). The histogram that is taken from Buras et al. (2006) is the asymptotic  $Y_e$  distribution  $p(Y_e)$  of the neutrino-processed ejecta during the first 468 ms after core bounce for a  $15 M_\odot$  progenitor star, obtained by their two-dimensional hydrodynamic simulation.

As can be seen, a variety of  $p$ -nuclei are produced with interesting amounts for  $Y_{ef} > 0.5$  models. The heavier  $p$ -nuclei (up to  $A \sim 130$ ) appear for the greater  $Y_{ef}$  models as well as for the larger  $M$  ( $= 2.0 M_\odot$ ) case (i.e., greater entropies, see Figs. 1-3). If we *assume* that the  $Y_e$  distribution by Buras et al. (2006) holds for the current models, the neutrino-driven winds may contribute the Galactic production of  $p$ -nuclei up to  $A \sim 110$  ( $^{74}\text{Se}$ ,  $^{78}\text{Kr}$ ,  $^{84}\text{Sr}$ ,  $^{92,94}\text{Mo}$ ,  $^{96,98}\text{Ru}$ ,  $^{102}\text{Pd}$ , and  $^{106,108}\text{Cd}$ ), which show considerable enhancements for  $Y_{ef} \approx 0.50 - 0.56$ . For the winds with  $L_\nu = 8 \times 10^{51}$  ergs s $^{-1}$  (Figure 13, *middle panels*), it can be seen also that the heavier  $p$ -nuclei are highly enhanced as  $Y_{ef}$  increases. For  $L_\nu = 2 \times 10^{51}$  ergs s $^{-1}$  (Figure 13, *bottom panels*), however, each  $p$ -process abundance reaches the maximum and decreases again as  $Y_{ef}$  increases. The reason is that the late winds in the current study cool down quickly below  $T_9 \sim 2$  as can be seen in Figures 2 and 3. As a result, most of the proton-rich abundances produced during the  $rp$ -process phase ( $T_9 \approx 3 - 2$ , Fig. 7, *bottom left*) suffer neutron capture to *neutron-rich* isotopes (Fig. 7, *bottom right*), regardless of the large  $Y_{ef}$  as well as the high entropy.

For  $Y_{ef} \approx 0.46 - 0.49$ , some light  $p$ -nuclei ( $^{74}\text{Se}$ ,  $^{78}\text{Kr}$ ,  $^{84}\text{Sr}$ , and  $^{92}\text{Mo}$ ) are enhanced with interesting amounts (Fig. 13). Of particular importance is the production of  $^{92}\text{Mo}$  as discussed in § 3.4. Hoffman et al. (1996) showed that a neutrino-driven wind having  $Y_e \gtrsim 0.484$  cures the  $N = 50$  overproduction (mostly  $^{90}\text{Zr}$ ), which is replaced

with the production of  $^{92}\text{Mo}$ . This strictly limited  $Y_e$  range is due to the competition between the production of  $^{90}\text{Zr}$  (as the seed of  $^{92}\text{Mo}$ ) in more neutron-rich winds and the concentration of protons (needed for the  $^{92}\text{Mo}$  production) in less neutron-rich winds. In the current study, the mass-averaged abundance of  $^{92}\text{Mo}$  with respect to its solar value overcomes that of  $^{90}\text{Zr}$  for wider range of  $Y_{ef}$  ( $\approx 0.46 - 0.49$ , Fig. 13, *top panels*). The reason is that the abundances are *mass averaged* over wide range of  $L_\nu$ , not from a *single* wind trajectory. In particular, the earlier winds experience longer durations at  $T_9 \approx 4 - 3$ , at which the  $^{92}\text{Mo}$  abundance is greatly enhanced (§ 3.4). In fact, for a specific wind, the enhancement of  $^{92}\text{Mo}$  is limited to a smaller  $Y_{ef}$  range as can be seen in Figure 13 (*middle and bottom panels*). In addition, the position of  $Y_{ef}$  at which the  $^{92}\text{Mo}$  abundance takes the maximum shifts toward 0.5 for lower  $L_\nu$  (i.e., later winds). This is a consequence that the later winds cool down quickly below  $T_9 \approx 4 - 3$ , thus the proton richness (i.e., larger  $Y_e$ ) is more important. In some later winds, relatively high entropies drive the material to form the QSE cluster that contains  $^{90}\text{Zr}$  even with small neutron excess ( $Y_{ef} \approx 0.49 - 0.50$ ), resulting in the enhancement of  $^{92}\text{Mo}$  (Fig. 13, *middle right and bottom panels*).

The mass fractions of  $p$ -nuclei with respect to their solar values (Anders & Grevesse 1989) are also shown as functions of  $L_\nu$  in Figure 14, for selected winds ( $M = 1.4 M_\odot$ ; *left panels*,  $M = 2.0 M_\odot$ ; *right panels*,  $Y_{e0} = 0.48$ ; *top panels*,  $Y_{e0} = 0.60$ ; *bottom panels*). For the winds with  $Y_{e0} = 0.48$  ( $Y_{ef} \approx 0.48$ , as representative of slightly neutron-rich winds),  $^{92}\text{Mo}$  is greatly enhanced at relatively early times ( $L_\nu > 1 \times 10^{52}$  ergs s $^{-1}$ , i.e.,  $t_{\text{pb}} < 0.8$  s). This is due to the slow decrease of the temperature in the early winds at  $T_9 \approx 4 - 3$ , in which  $^{92}\text{Mo}$  is most enhanced (§ 3.4). It should be cautioned that the steady wind approximation assumed in this study may not hold during the very early (*bubble*) phase ( $t_{\text{pb}} < 0.5$  s). However, it is likely that the material ejected as *bubbles* expand more slowly (e.g., Buras et al. 2006), and experiences longer time at  $T_9 \approx 4 - 3$  in which  $^{92}\text{Mo}$  might enhance to a similar (or more) degree. For the winds with  $Y_{e0} = 0.60$  ( $Y_{ef} \approx 0.54 - 0.56$ , as representative of proton-rich winds),  $p$ -nuclei are enhanced at rel-

atively later times ( $L_\nu < 1 \times 10^{52}$  ergs s $^{-1}$ , i.e.,  $t_{\text{pb}} > 0.8$  s), where the steady wind approximation may hold (Figure 14, *bottom panels*). This is also consistent to the results by Pruet et al. (2006), which showed no significant production of  $p$ -nuclei in the bubbles. Note that no  $p$ -nuclei are produced in the very late winds ( $L_\nu < 2 \times 10^{51}$  ergs s $^{-1}$ , i.e.,  $t_{\text{pb}} > 4$  s), in which the matter is assumed to be rather neutron rich (Fig. 4, *top panel*).

#### 4.2. Mass- $Y_e$ -averaged Yields

In reality, the neutrino-heated matter must have a certain distribution of  $Y_e$  when the multi-dimensional effects are taken into account. The problem is, of course, the unknown mechanism of core-collapse supernovae, which governs the hydrodynamic and thermodynamic histories of the neutrino-driven winds. Among a number of *artificially* induced explosion models, only the two-dimensional calculation with accurate neutrino transport by Buras et al. (2006) provides us a reliable  $Y_e$  distribution of the neutrino-processed material. The explosion in their simulation was obtained by omitting the velocity-dependent terms from the neutrino momentum equation. This led to the increase of the neutrino energy deposition in the heating region by a few 10%, which converted a failed model into an exploding one. The  $Y_e$  distribution  $p(Y_e)$  of the neutrino-processed ejecta during the first 468 ms after core bounce for a  $15 M_\odot$  progenitor star obtained by Buras et al. (2006) is overlaid in Figure 13. The histogram has the maximum at  $Y_e \approx 0.5$  and dominates in the proton-rich side.

To test the contributions of the winds for  $M = 1.4 M_\odot$  and  $2.0 M_\odot$  models, the mass-averaged yields for each  $Y_{e0}$  model (Fig. 13, *top panels*) are further  $Y_e$ -averaged ( $\sim 2000$  winds in total for each  $M$ ) with  $p(Y_e)$ , *assuming* this distribution to be representative of neutrino-driven winds. Needless to say, there is no guarantee that this distribution holds for the current wind models (at  $t_{\text{pb}} = 4$  s) for both  $M = 1.4 M_\odot$  and  $2.0 M_\odot$  cases. However, this is only the case obtained by a multi-dimensional hydrodynamic calculation with *accurate* neutrino transport that is essential to predict the  $Y_e$  distribution of the neutrino-heated ejecta. It may be, therefore, interesting to see the possible contributions to the Galactic chemical evolution with this  $p(Y_e)$ , keeping in mind that a more con-

sistent estimation of  $p(Y_e)$  will be needed in the future study.

The resulting abundances with respect to their solar values are shown in Figure 15 for  $M = 1.4 M_\odot$  (*top panel*) and  $2.0 M_\odot$  (*bottom panel*) models as functions of mass number. The abundances smaller than  $X_{\text{ej}}/X_\odot < 100$  are omitted here. The even- $Z$  and odd- $Z$  isotopes for a given element are denoted by circles and triangles, respectively, which are connected by lines. The  $p$ -nuclei are marked with filled symbols. The dotted horizontal lines indicate a “normalization band” (Woosley et al. 1994) between the largest production factor ( $^{100}\text{Mo}$  for  $M = 1.4 M_\odot$  and  $^{92}\text{Mo}$  for  $M = 2.0 M_\odot$ ) and that by a factor of ten less than that, along with the median value (*dashed line*). This band is taken to be representative of the uncertainty in the nuclear data involved.

When compared with the results in which the mass average is only for  $L_\nu \geq 2 \times 10^{51}$  ergs s $^{-1}$  (Fig. 17, *top panels*), it is clear that the later winds for  $L_\nu < 2 \times 10^{51}$  ergs s $^{-1}$  contribute to only the  $r$ -nuclei with  $A > 90$  but to  $p$ -nuclei. Figure 15 implies that there exists a correlation between the production of  $p$ -nuclei and  $r$ -nuclei. That is, the higher entropy model ( $M = 2.0 M_\odot$ ) produces heavier  $p$ -nuclei (up  $A \sim 110$ ) and  $r$ -nuclei (up to  $A \sim 190$ ) in a *single* event. This might be true, since both the  $rp$ -process and  $r$ -process favor the high entropy conditions. It would be premature to conclude that, however, when considering the highly uncertain late-time evolution of neutrino-driven winds. It is interesting to note that the overproduction of  $N = 50$  nuclei  $^{88}\text{Sr}$ ,  $^{89}\text{Y}$ , and  $^{90}\text{Zr}$  seen in the previous  $r$ -process studies (Woosley et al. 1994; Wanajo et al. 2001) are now replaced with the moderate production of  $^{92}\text{Mo}$ . Figure 16 compares the results when  $M$  is replaced to  $1.6 M_\odot$  (*top panel*) or  $1.8 M_\odot$  (*top panel*). The higher entropy ( $\sim 20\%$  for the former and  $\sim 50\%$  for the latter) with respect to the case of  $M = 1.4 M_\odot$  (Fig. 15, *top panel*) results in the production of  $p$ -nuclei with higher mass numbers (and of  $r$ -nuclei). This shows that the moderate entropy of  $\sim 60 - 80 N_A k$  in early winds ( $\sim 1$  s) is sufficient for the reasonable production of light  $p$ -nuclei up to  $A \sim 100 - 110$ .

Hereafter, only the winds for  $L_\nu \geq 2 \times 10^{51}$  ergs s $^{-1}$  ( $t_{\text{pb}} \leq 4$  s) are considered, in which the  $p$ -nuclei are produced. Note that the pro-

duction of  $^{64}\text{Zn}$  that is the dominant stable zinc isotope (but its origin is unknown, see Hoffman et al. 1996; Umeda & Nomoto 2002; Pruet et al. 2005; Fröhlich et al. 2006a) is about 10 times smaller than the lower normalization band, much smaller than expected in Hoffman et al. (1996, see also Fig. 13). The contributions to the production of  $^{45}\text{Sc}$  and  $^{49}\text{Ti}$  are not important either, which are suggested to be produced in the earlier ejecta (Pruet et al. 2005; Fröhlich et al. 2006a).

Figure 17 compares the results with (*top panels*) and without (*bottom panels*) neutrino reactions (eqs. [1]-[6]) for the  $M = 1.4 M_\odot$  (*left panels*) and  $2.0 M_\odot$  (*right panels*) models. As can be seen, the production of almost all  $^{92}\text{Mo}$  and some portions of  $^{74}\text{Se}$ ,  $^{78}\text{Kr}$ , and  $^{84}\text{Sr}$  are not due to the effect of neutrino reactions. This can be also seen in Figure 18, which compares the results from only neutron-rich (*top panels*) or proton-rich (*bottom panels*) winds for the  $M = 1.4 M_\odot$  (*left panels*) and  $2.0 M_\odot$  (*right panels*) models.  $^{92}\text{Mo}$  is highly overproduced in the mass average of neutron-rich winds, which is, on the contrary, somewhat underproduced in the proton-rich winds compared to other light  $p$ -nuclei (e.g.,  $^{74}\text{Se}$ ,  $^{78}\text{Kr}$ ,  $^{84}\text{Sr}$ ,  $^{94}\text{Mo}$ , and  $^{96,98}\text{Ru}$ ). Hence, the bulk of  $^{92}\text{Mo}$  originates from the slightly neutron-rich winds ( $Y_{ef} \approx 0.46 - 0.50$ ), while other  $p$ -nuclei from mainly proton-rich winds.

When we look at the top panels of Figure 17 again, the  $p$ -nuclei up to  $^{92}\text{Mo}$  and  $^{108}\text{Cd}$  for  $M = 1.4 M_\odot$  and  $2.0 M_\odot$  models, respectively, fall within the normalization band, which are regarded to be the dominant species produced by each event. It is interesting to note that the contributions to  $^{94}\text{Mo}$ ,  $^{96,98}\text{Ru}$ , and  $^{102}\text{Pd}$  for  $M = 1.4 M_\odot$  and  $^{112,114,115}\text{Sn}$ , and  $^{113}\text{In}$  for  $M = 2.0 M_\odot$  are marginal. The ejected masses by winds during the first 20 s are  $3.0 \times 10^{-3} M_\odot$  and  $1.2 \times 10^{-3} M_\odot$  for the current  $M = 1.4 M_\odot$  and  $2.0 M_\odot$  models, respectively. Given that the progenitor mass for each case to be, e.g.,  $15 M_\odot$  and  $30 M_\odot$ , respectively, the overproduction factor is expressed as  $\sim 10^{-4} (X_{ej}/X_\odot)$ . The requisite overproduction factor for the nucleosynthetic event to be the major source in the solar system is  $\sim 10$  (Woosley et al. 1994), assuming that *all* the core-collapse supernovae produce the same amount of the isotope. This number increases (e.g.,  $\sim 100$ ) if a limited fraction of supernovae (e.g.,  $25-30 M_\odot$ ) contribute

to these light  $p$ -nuclei production (see Ishimaru & Wanajo 1999; Wanajo & Ishimaru 2006b, for the  $r$ -process elements). This is conceivable since the current nucleosynthesis results are highly dependent on the physical conditions such as entropy or  $Y_e$ . The overproduction factors of  $\sim 10 - 100$  (Fig. 17, *top panels* or Fig. 15) for the current models imply that the neutrino-driven winds can be potentially the major astrophysical site of these light  $p$ -nuclei.

## 5. Summary and Conclusions

In this study, the neutrino-induced  $rp$ -process in neutrino-driven winds has been investigated. The thermodynamic histories of winds were obtained from the semi-analytic models of the neutrino-driven winds that had been developed for the  $r$ -process study in previous works. The subsonic wind solutions with the nearly maximum mass ejection rates were taken in this study, for various neutrino luminosities ( $40 - 0.5 \times 10^{51} \text{ ergs s}^{-1}$ ) with the proto-neutron star masses of  $1.4 M_\odot$  and  $2.0 M_\odot$ . The latter ( $2.0 M_\odot$ ) was regarded as the test case of higher entropy winds (about a factor of two), which might be expected in more realistic hydrodynamic simulations of core-collapse supernovae. The nucleosynthesis calculations were performed for the wide range of the initial electron fractions ( $0.45 \leq Y_{e0} \leq 0.65$ ) including rather proton-rich compositions, motivated by recent hydrodynamic results. The main results of this study can be summarized as follows:

1. In the proton-rich winds, the proton capture can proceed beyond the iron-group nuclei, by bypassing the known  $\beta^+$ -waiting point nuclei (e.g.,  $^{64}\text{Ge}$ ) via  $(n, p)$  reactions, as also suggested by recent works (Fröhlich et al. 2006a,b; Pruet et al. 2006; Wanajo 2006). These neutrons are continuously supplied from the anti-electron neutrino capture on abundant free protons.
2. The neutrino-induced  $rp$ -process leads to the production of some light  $p$ -nuclei, even with moderate entropy ( $\sim 50 N_A k$ ) that can be found in the early winds ( $t_{\text{pb}} \sim 1 \text{ s}$ ) from the neutron star with  $1.4 M_\odot$ . The production of  $p$ -nuclei is, however, highly dependent on the entropy in the wind, which affects the proton-to-seed abundance ratio  $Y_p/Y_h$  at the beginning of the  $rp$ -process. In the high entropy winds ( $\sim 100 N_A k$ )

with  $M = 2.0 M_{\odot}$ , the nuclear flow proceeds to  $Z \approx 50$ , resulting in the production of  $p$ -nuclei up to  $A \sim 130$ .

3. The production of  $p$ -nuclei is also highly sensitive to the proton richness of the wind material. In the slightly proton-rich winds ( $Y_e \sim 0.50 - 0.52$ ), only the lightest  $p$ -nuclei ( $^{74}\text{Se}$ ,  $^{78}\text{Kr}$ , and  $^{84}\text{Sr}$ ) are produced. The higher  $p$ -nuclei up to  $A \sim 130$  are synthesized with interesting amounts as  $Y_e$  rises to  $\sim 0.56$ .

4. The termination of the  $rp$ -process is due to the increasing Coulomb barrier for the heaviest nuclei in the nuclear flow, *not* due to the exhaustion of free protons. The decrease of the temperature below  $\sim 2 \times 10^9 \text{ K}$  owing to the expansion of the ejecta is also a cause of the termination. The supply of neutrons by the neutrino capture on protons is sufficient throughout the  $rp$ -process phase. Hence the dilution of the neutrino flux by the expansion of matter is not the principal reason for the termination of the  $rp$ -process in the current wind models.

5. Few  $p$ -nuclei beyond  $A \sim 130$  are produced by the neutrino-induced  $rp$ -process, owing to the increasing Coulomb barrier for heavier nuclei. The high entropy ( $\sim 200 N_A k$ ) or highly proton-rich ( $Y_e \sim 0.6$ ) wind results in driving the nuclear abundances to the  $\beta$ -stability or even the neutron-rich region, when the temperature drops below  $T_9 \sim 2$ . In this case, a variety of neutron-rich isotopes, which are generally assigned to  $s$ -nuclei or  $r$ -nuclei, are synthesized even in the proton-rich compositions.

6.  $^{92}\text{Mo}$  is produced with interesting amounts in the slightly neutron-rich winds ( $Y_e \sim 0.46 - 0.49$ ), much more than in the proton-rich winds. This is due to the proton capture reactions at  $T \sim 4 - 3 \times 10^9 \text{ K}$ , which carry a portion of the nuclear abundances from the abundant  $^{90}\text{Zr}$  to  $^{92}\text{Mo}$ . The amount of the produced  $^{92}\text{Mo}$  is, however, highly dependent on the thermodynamic history of the wind.

7. The neutrino-driven winds can be the origin of some light  $p$ -nuclei, at least of  $^{74}\text{Se}$ ,  $^{78}\text{Kr}$ ,  $^{84}\text{Sr}$ , and  $^{92}\text{Mo}$ , and likely of  $^{94}\text{Mo}$ ,  $^{96,98}\text{Ru}$ ,  $^{102}\text{Pd}$ , and  $^{106,108}\text{Cd}$ , supplemented by the production of  $^{92}\text{Mo}$  in the slightly neutron-rich compositions. In particular, this can be the unique astrophysical site responsible for the production of the proton-

rich Mo and Ru isotopes. The heavier  $p$ -nuclei ( $A > 110$ ) may have another origin, most likely the O/Ne layers in core-collapse supernovae (Prantzos et al. 1990; Rayet et al. 1995). Note that the  $p$ -nuclei synthesized in neutrino-driven winds are regarded as *primary*. This is contrast to those produced in the O/Ne layers, which need the  $s$ -process seed abundances and thus regarded as *secondary*.

Note that the neutrino-induced  $rp$ -process in the current study may not contribute to the production of any *elements*, since the fraction of  $p$ -process isotopes for a given element is generally an order of one percent. Therefore, it would be challenging to confirm the occurrence of the neutrino-induced  $rp$ -process by spectroscopic studies of extremely metal-poor stars, which are expected to preserve the nucleosynthetic signature from a single (or a few) supernova (e.g., Ishimaru & Wanajo 1999; Wanajo & Ishimaru 2006b). Analysis of the isotope anomalies in some elements found in primitive meteorites (e.g., Arnould & Goriely 2003) or measurements of Galactic cosmic-rays might provide us some clues.

At the end of this investigation, it should be cautioned that the nucleosynthesis calculations in the current study are based on a schematic formulation of neutrino-driven winds, which must be in fact closely related to the unknown mechanism of core-collapse supernovae. In addition, the estimation of the  $p$ -nuclei production in each event (i.e., the core-collapse supernova that leaves the proto-neutron star with  $1.4 M_{\odot}$  or  $2.0 M_{\odot}$ ) was based on the  $Y_e$  distribution during the *bubble* (not wind) phase, obtained from one specific hydrodynamic simulation (Buras et al. 2006). Therefore, the current results should *not* be regarded as the quantitative predictions that is to be used for the Galactic chemical evolution study.

Nevertheless, the current study provides us some notable implications. First, it is likely that the neutrino-induced  $rp$ -process takes place in *all* core-collapse supernovae to some extent, even with a moderate entropy. In this sense, other astrophysical sites than standard core-collapse events, e.g., collapsar jets or disk winds formed around a black hole, which are associated to gamma-ray bursts, can be the astrophysical site for the neutrino-induced  $rp$ -process. Second, details of the nucleosynthesis process are presented for se-

lected winds, which will be useful for the future experimental studies of proton-rich nuclei far from the  $\beta$ -stability. In particular, core-collapse supernovae no doubt eject the nucleosynthetic products that contribute to the Galactic chemical evolution of heavy nuclei. This is in contrast to X-ray bursts, which is unlikely to contribute the Galactic chemical evolution. Therefore the experimental estimations can be easily tested by comparing the nucleosynthesis calculations to, e.g., the solar compositions. Third, the systematic calculations for the wide (but reasonable) ranges of the neutrino luminosities and the electron fractions enable us to make a meaningful comparison with the solar abundances. In particular, a notable aspect is that  $^{92}\text{Mo}$  has another origin (i.e., neutron-rich winds) while other light  $p$ -nuclei are mainly synthesized by the  $rp$ -process (i.e., in proton-rich winds) even in a *single* event. This will serve unique constraints to the fluid dynamics of the early supernova ejecta.

This work was supported in part by a Grant-in-Aid for Japan-France Integrated Action Program (SAKURA) from the Japan Society for the Promotion of Science, and Scientific Research (17740108) from the Ministry of Education, Culture, Sports, Science, and Technology of Japan.

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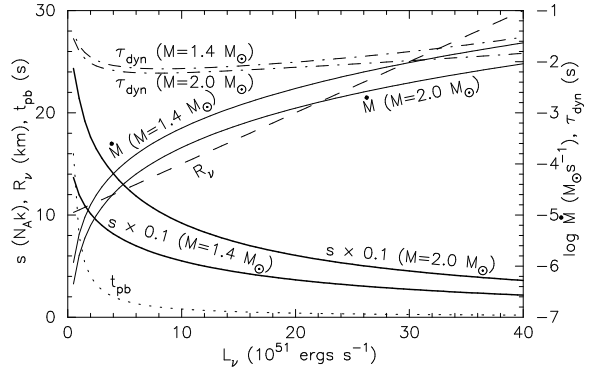


Fig. 1.— Model parameters ( $R_\nu, t_{pb}, \dot{M}$ ) of the current neutrino-driven winds are shown as functions of  $L_\nu$ . Also denoted are the obtained entropies ( $s$ ) and dynamic timescales ( $\tau_{dyn}$ ) for  $1.4 M_\odot$  and  $2.0 M_\odot$  cases.



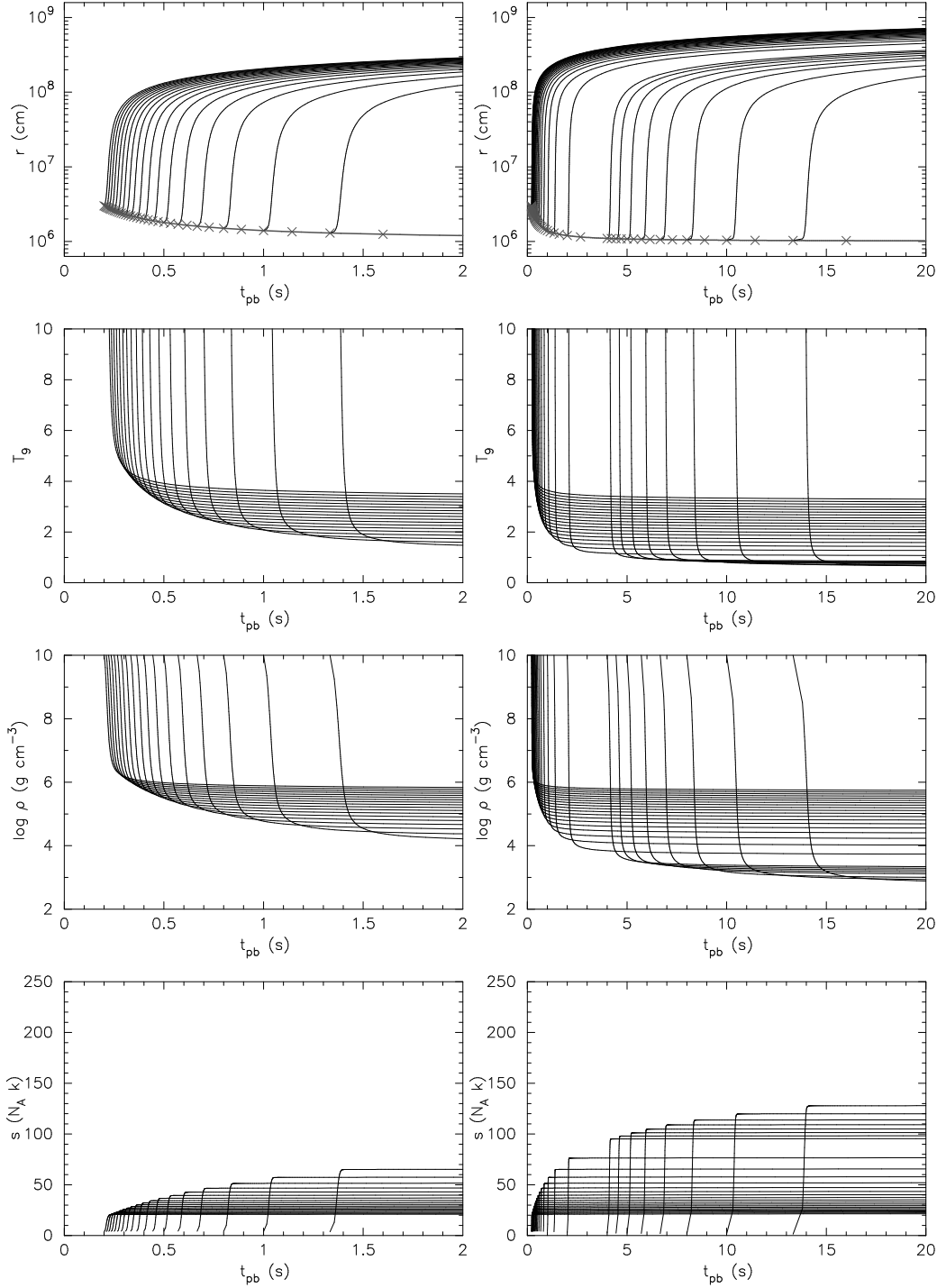


Fig. 2.— Time variations of radius, temperature, density, and entropy for selected (odd-numbered) wind trajectories with the  $M = 1.4 M_{\odot}$  model ( $t_{\text{pb}} \leq 2$  s and  $t_{\text{pb}} \leq 20$  s for *left* and *right panels*, respectively). The evolution of the neutrino sphere is denoted by the grey lines along with the starting point for each wind (crosses) in top panels.

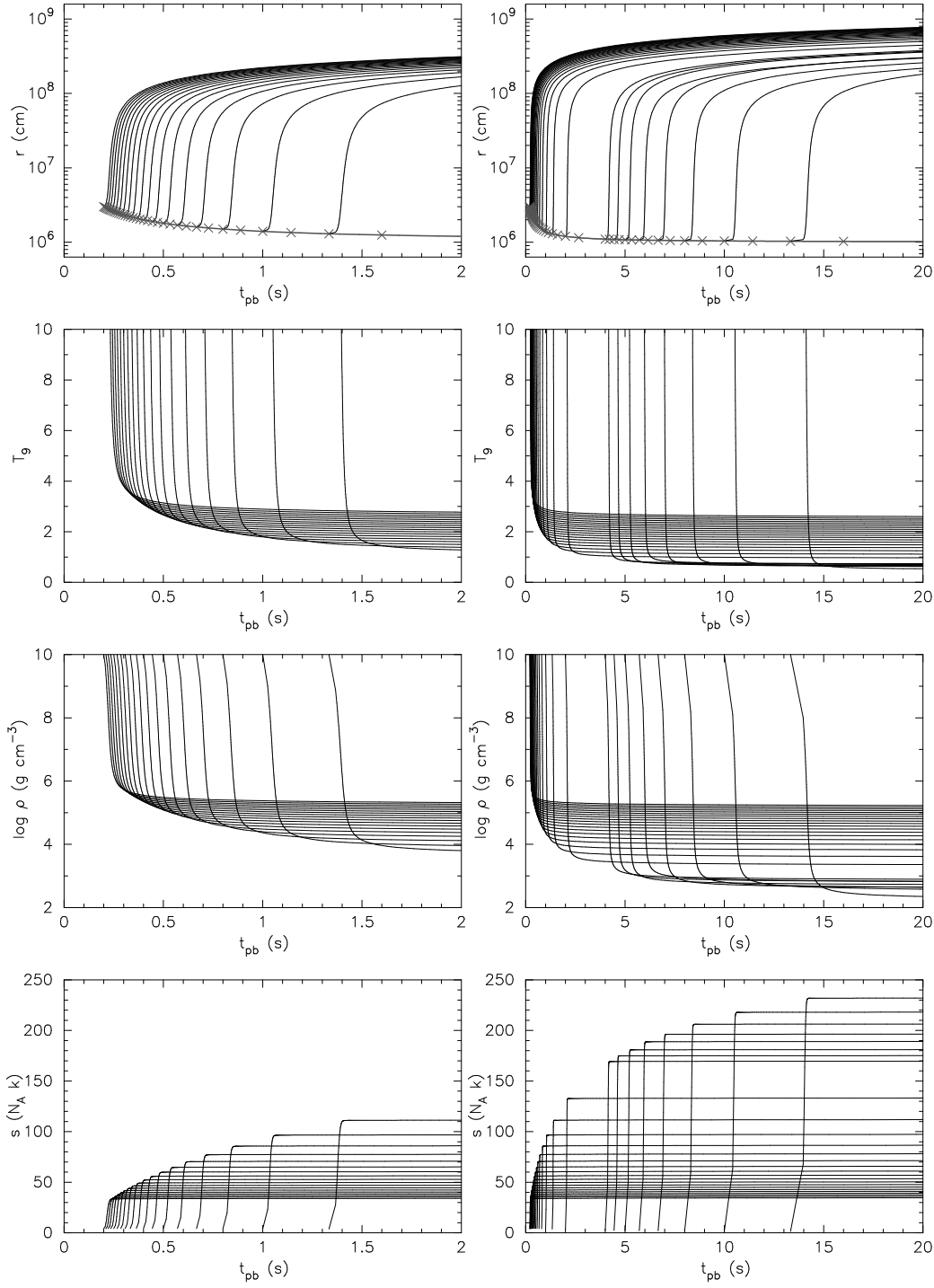


Fig. 3.— Same as Figure 2, but for the  $M = 2.0 M_{\odot}$  model.

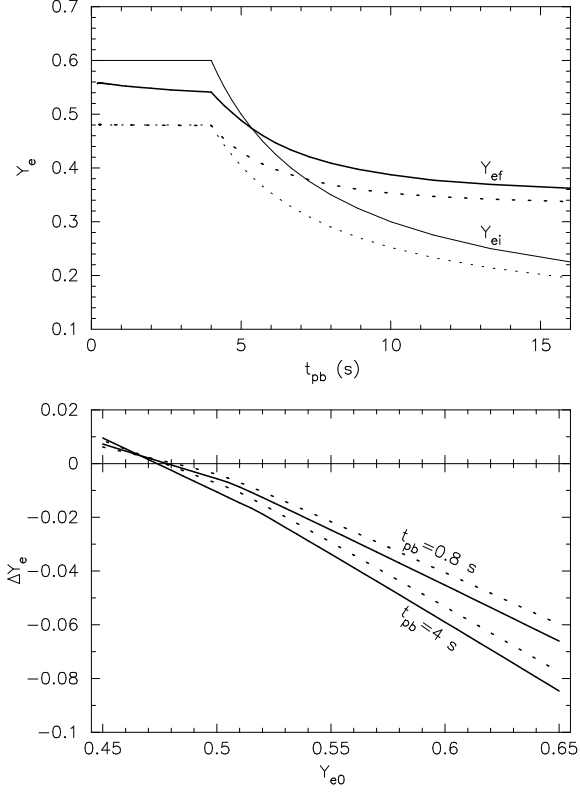


Fig. 4.— *Top*:  $Y_e$  at  $T_9 = 9$  ( $Y_{ei}$ , *thin lines*) and at  $T_9 = 3$  ( $Y_{ef}$ , *thick lines*) as functions of  $t_{pb}$ . The solid and dotted lines denote the results for  $M = 2.0 M_\odot$  with  $Y_{e0} = 0.60$  and  $M = 1.4 M_\odot$  with  $Y_{e0} = 0.48$ , respectively. *Bottom*: Differences of  $Y_e$  ( $\Delta Y_e \equiv Y_{ei} - Y_{ef}$ ) at  $t_{pb} = 0.8$  s and  $4.0$  s as functions of  $Y_{e0}$ , for  $M = 1.4 M_\odot$  (*dotted lines*) and  $2.0 M_\odot$  (*solid lines*).

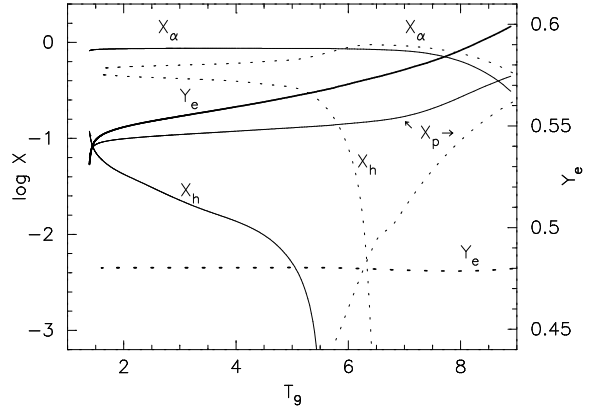


Fig. 5.— Variations of  $Y_e$  (*thick lines*) and the mass fractions (*thin lines*) of neutrons ( $X_n$ ), protons ( $X_p$ ),  $\alpha$  particles ( $X_\alpha$ ), and heavy nuclei ( $X_h$ ) as functions of  $T_9$ . The solid and dotted lines denote the results for the wind trajectories W201060 and W141048 (see the text and footnote 1), respectively.

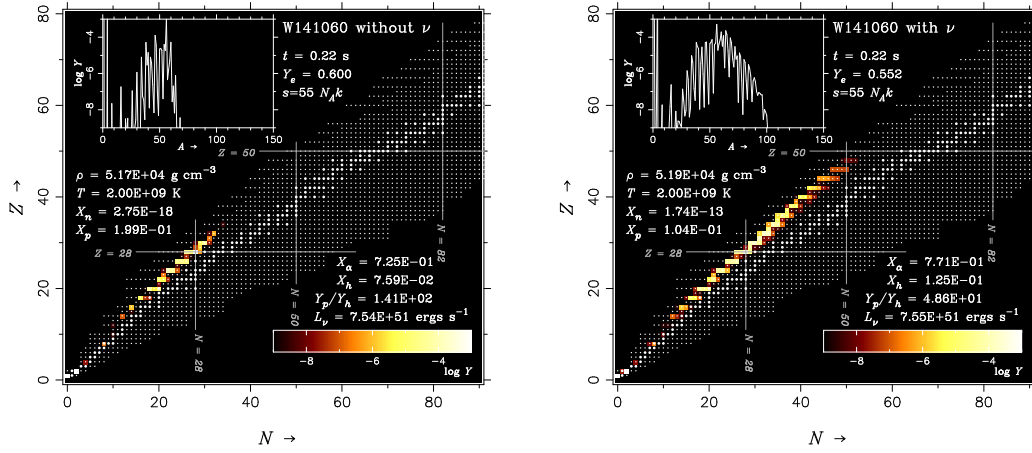


Fig. 6.— Snapshots of the nucleosynthesis calculations at  $t = 0.22$  s for the wind trajectory of W141060, in which the neutrino-induced reactions (eqs. [1]-[6]) are turned off (*left panel*) and on (*right panel*). The temperature decreases to  $T_9 \approx 2$  at this time. The abundances are color coded in the nuclide chart. The nuclei included in the reaction network are denoted by dots, with the stable isotopes represented by large dots. The abundance curve as a function of mass number is shown in the upper left for each panel.

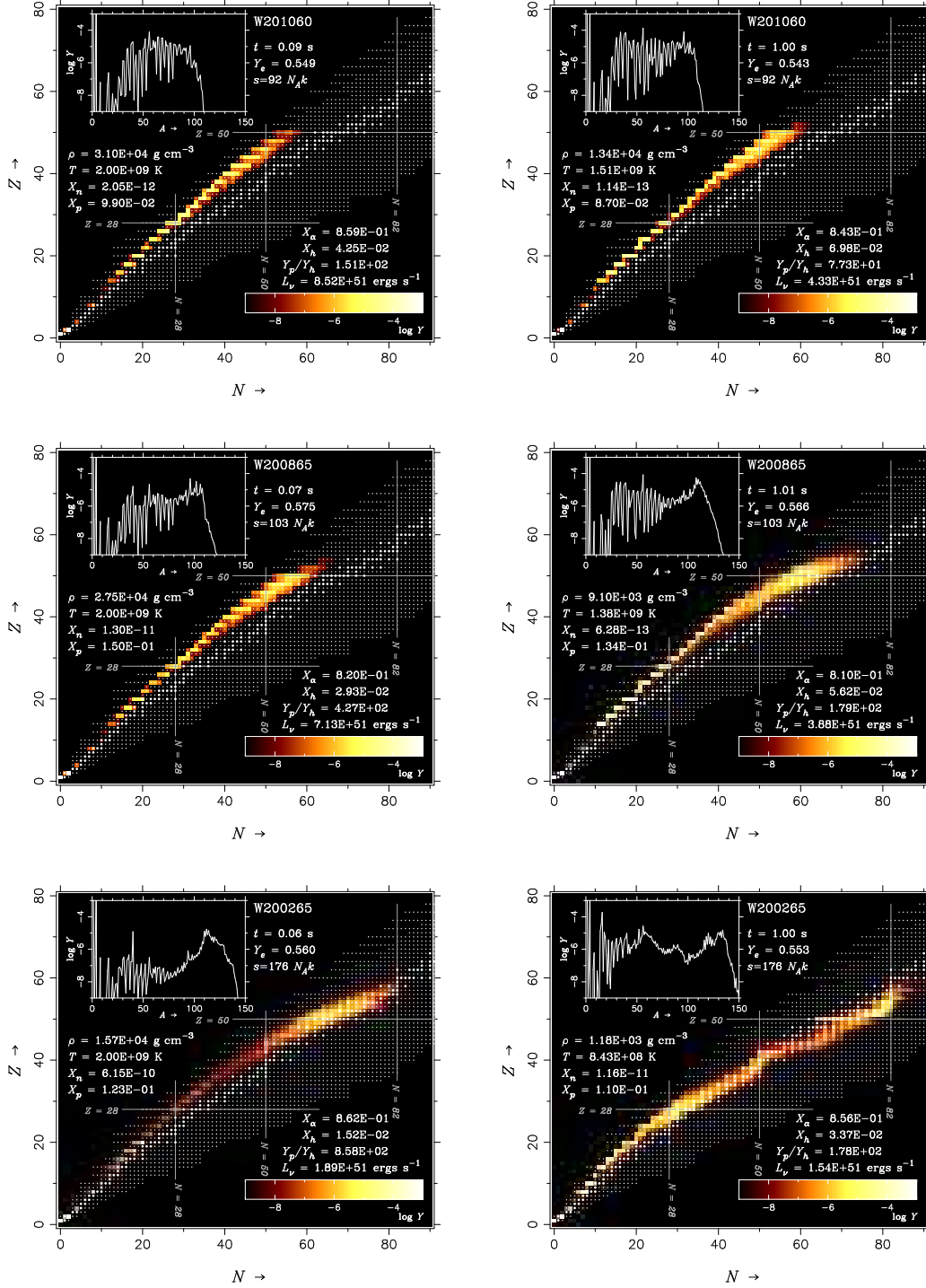


Fig. 7.— Same as Figure 6, but for the wind trajectories of W201060 (*top*), W200865 (*middle*), and W200265 (*bottom*). Left and right panels are the snapshots at  $T_9 \approx 2.0$  and  $t_{pb} \approx 1.0$  s, respectively. Neutrino-induced reactions (eqs. [1]-[6]) are included for all cases.

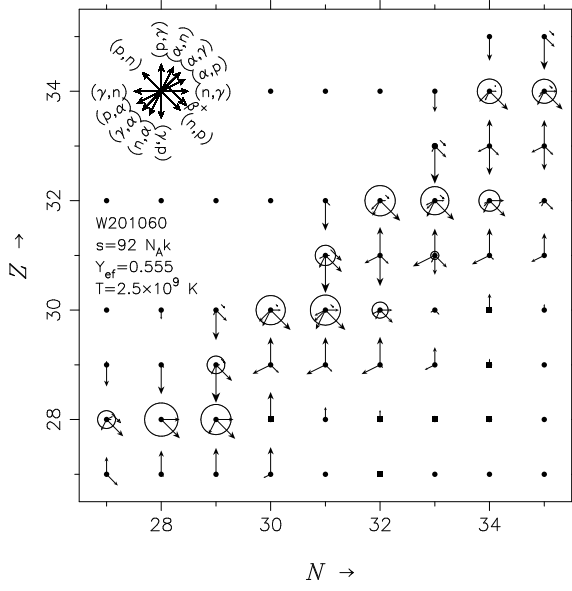


Fig. 8.— Nuclear flows defined by equation (9) (*arrows*) and the abundances (*circles*) in logarithmic scale for the wind trajectory of W201060 at  $T_9 = 2.5$ , for those greater than  $10^{-5}$ . The flows by  $\beta^+$ -decays are denoted by off-centered arrows. The nuclei included in the reaction network are denoted by dots, with the stable isotopes represented by squares.

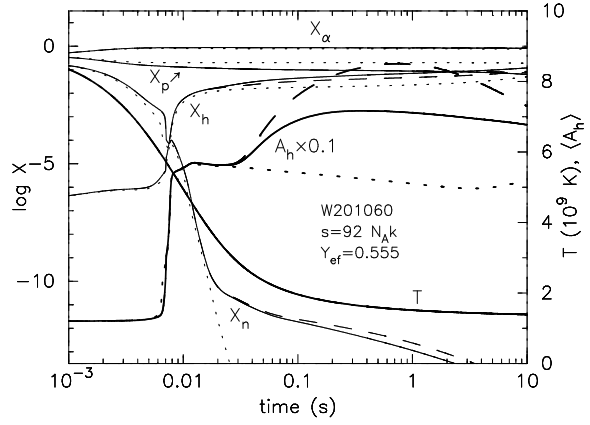


Fig. 9.— Time variations of the mass fractions (*thin lines*) of neutrons  $X_n$ , protons  $X_p$ ,  $\alpha$  particles  $X_\alpha$ , and heavy nuclei  $X_h$  for the wind trajectory W201060. The solid, dashed, and dotted lines denote the results with all neutrino-induced reactions (eqs. [1]-[6]), neutrino capture on free nucleons only (eqs. [1] and [2]), and no neutrino-induced reactions, respectively. Also shown are the average mass number of heavy nuclei  $A_h$  and the temperature (*thick lines*).

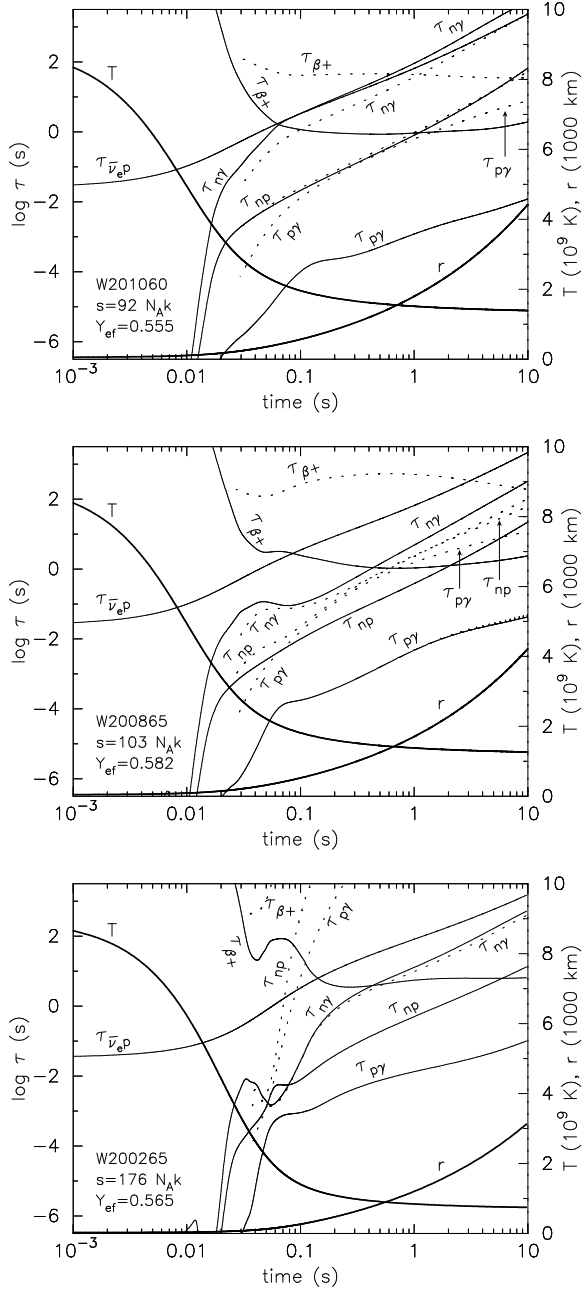


Fig. 10.— Time variations of the mean lifetimes for  $\beta^+$ -decay,  $(n, \gamma)$ ,  $(p, \gamma)$ , and  $(n, p)$  reactions, and neutrino capture on protons for the wind trajectories of W201060 (*top*), W200865 (*middle*), and W200265 (*bottom*), defined by equations (12)-(16). The solid and dotted lines denote the lifetimes for  $Z \geq 2$  and  $Z \geq 48$  nuclei, respectively. For the latter, the values for only  $T_9 < 3$  are shown, in which these nuclei are synthesized by the  $rp$ -process. Also shown are the temperature and the distance from the center of the neutron star (*thick lines*).

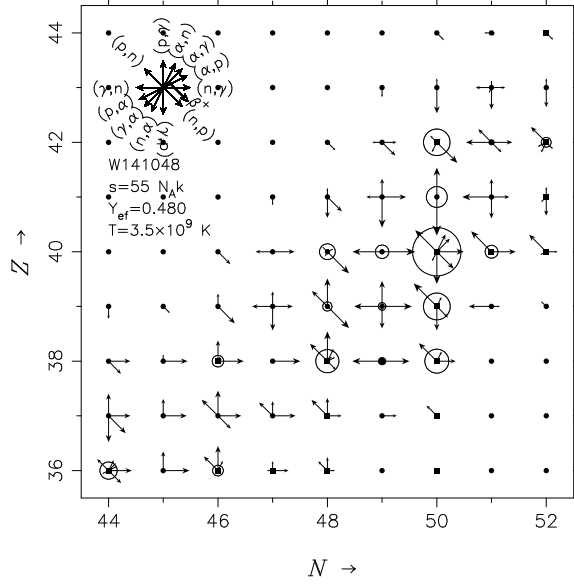


Fig. 11.— Same as Figure 8, but for the wind trajectory of W141048.

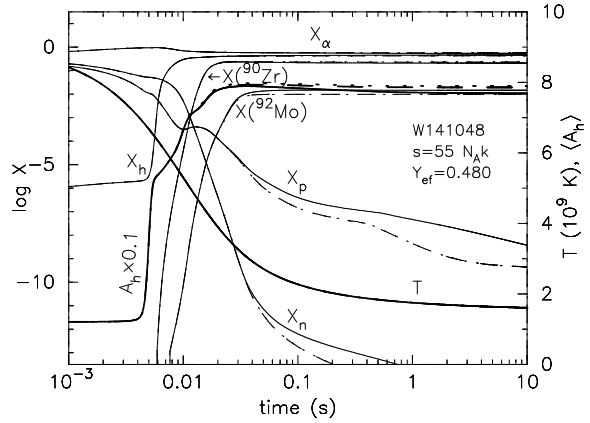


Fig. 12.— Same as Figure 9, but for the wind trajectory of W141048. The mass fractions of  $^{90}\text{Zr}$  and  $^{92}\text{Mo}$  are also plotted.

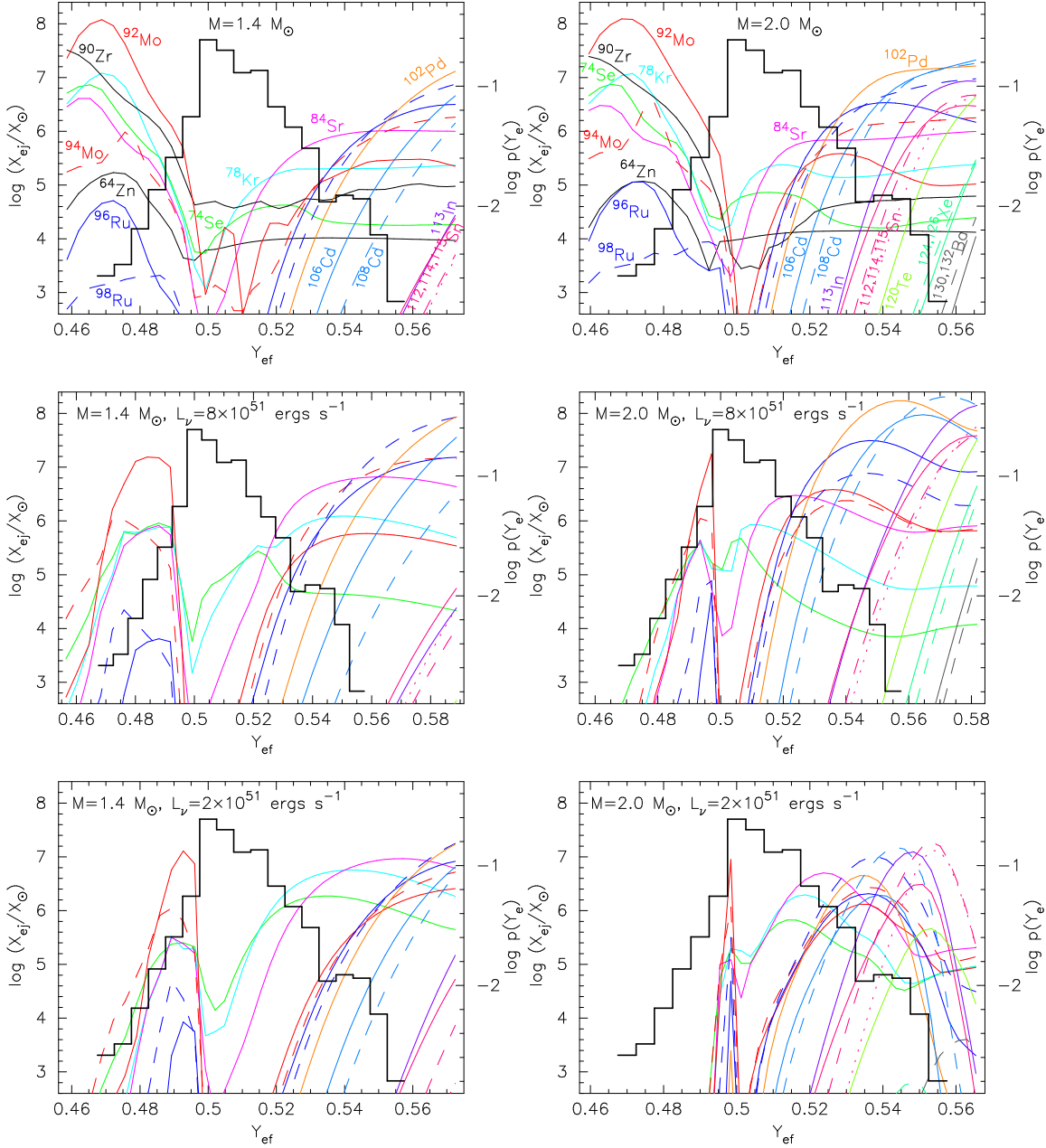


Fig. 13.— Mass fractions  $X_{ej}$  of  $p$ -nuclei with respect to their solar values ( $X_{\odot}$ , Anders & Grevesse 1989) as functions of  $Y_{ef}$  for  $M = 1.4 M_{\odot}$  (left) and  $2.0 M_{\odot}$  (right) models. Top panels show the mass-averaged results (see the text), where  $Y_{ef}$  is taken to be that at  $t_{pb} = 4$  s ( $L_{\nu} = 2 \times 10^{51}$  ergs  $s^{-1}$ ). The mass fractions of  $^{64}\text{Zn}$  and  $^{90}\text{Zr}$  are also plotted for comparison purposes. Middle and bottom panels show the results for the winds with  $L_{\nu} = 8 \times 10^{51}$  ergs  $s^{-1}$  and  $2 \times 10^{51}$  ergs  $s^{-1}$ , respectively. The histogram is the asymptotic  $Y_e$  distribution  $p(Y_e)$  of the neutrino-processed ejecta during the first 468 ms after core bounce for a  $15 M_{\odot}$  progenitor star taken from Buras et al. (2006).



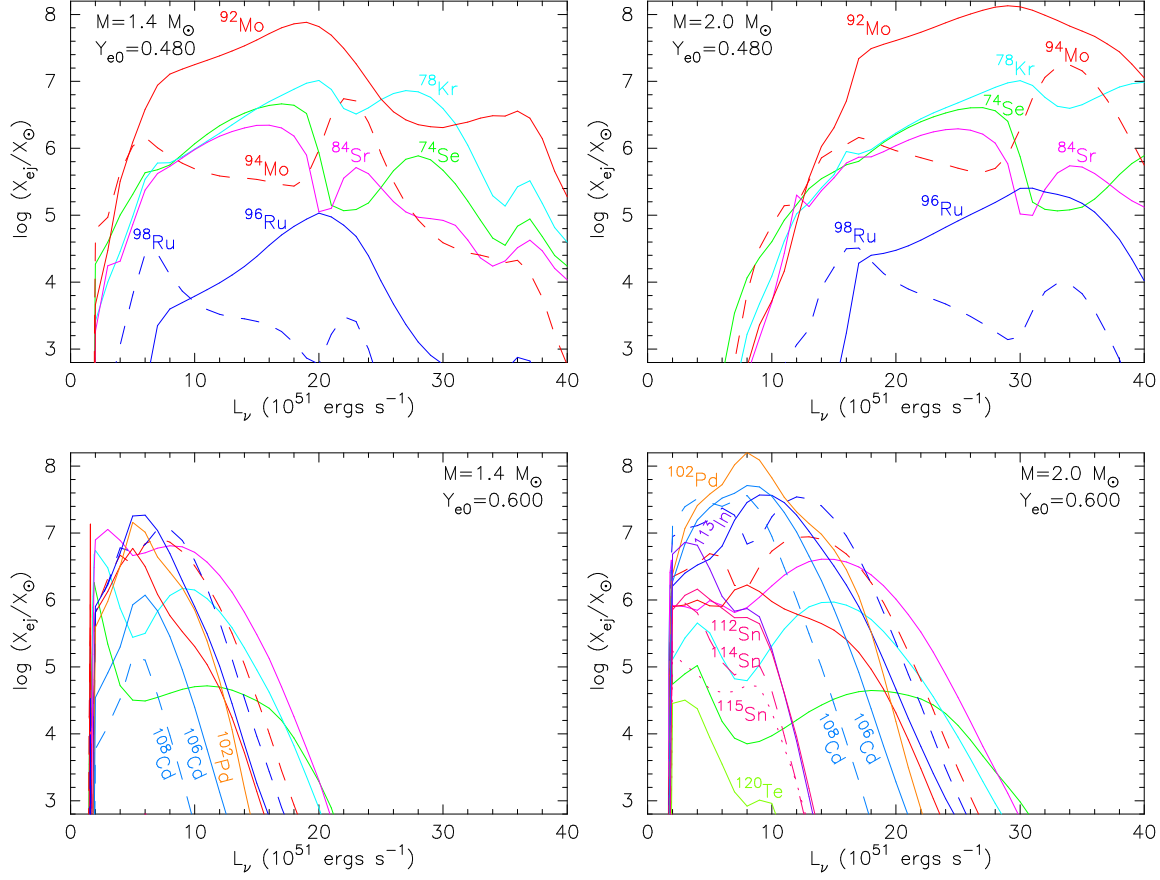


Fig. 14.— Mass fractions of  $p$ -nuclei with respect to their solar values (Anders & Grevesse 1989) as functions of  $L_\nu$ , for the selected cases ( $M = 1.4 M_\odot$ ; left,  $M = 2.0 M_\odot$ ; right,  $Y_{e0} = 0.48$ ; top,  $Y_{e0} = 0.60$ ; bottom).

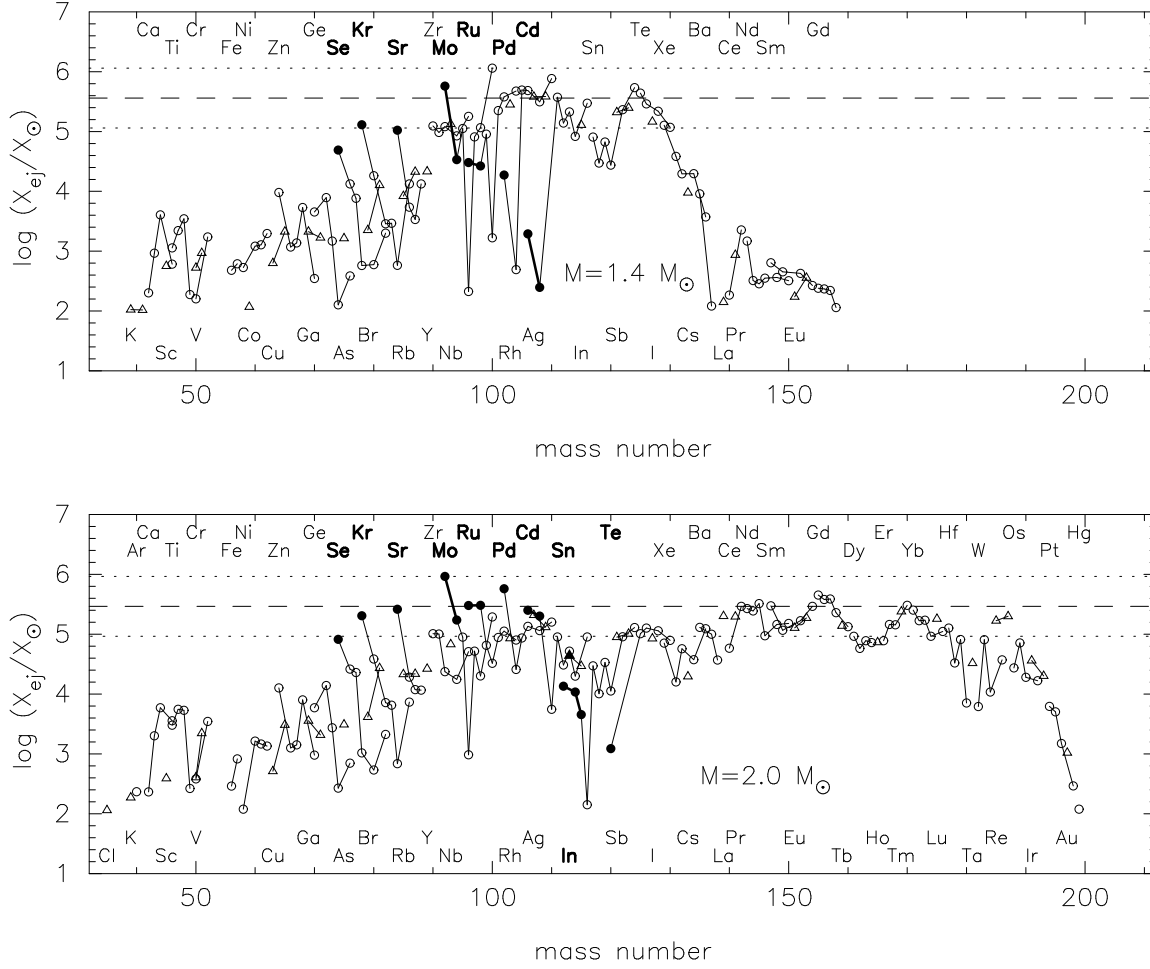


Fig. 15.— Mass- $Y_e$ -averaged abundances with respect to their solar values (Anders & Grevesse 1989) for  $M = 1.4 M_{\odot}$  (top) and  $2.0 M_{\odot}$  (bottom) models as functions of mass number (see the text). The abundances smaller than  $X_{ej}/X_{\odot} < 100$  is omitted here. The isotopes (after decay) are denoted by open circles (even- $Z$ ) and triangles (odd- $Z$ ). The  $p$ -nuclei are denoted with filled symbols. The solid lines connect isotopes of a given element.

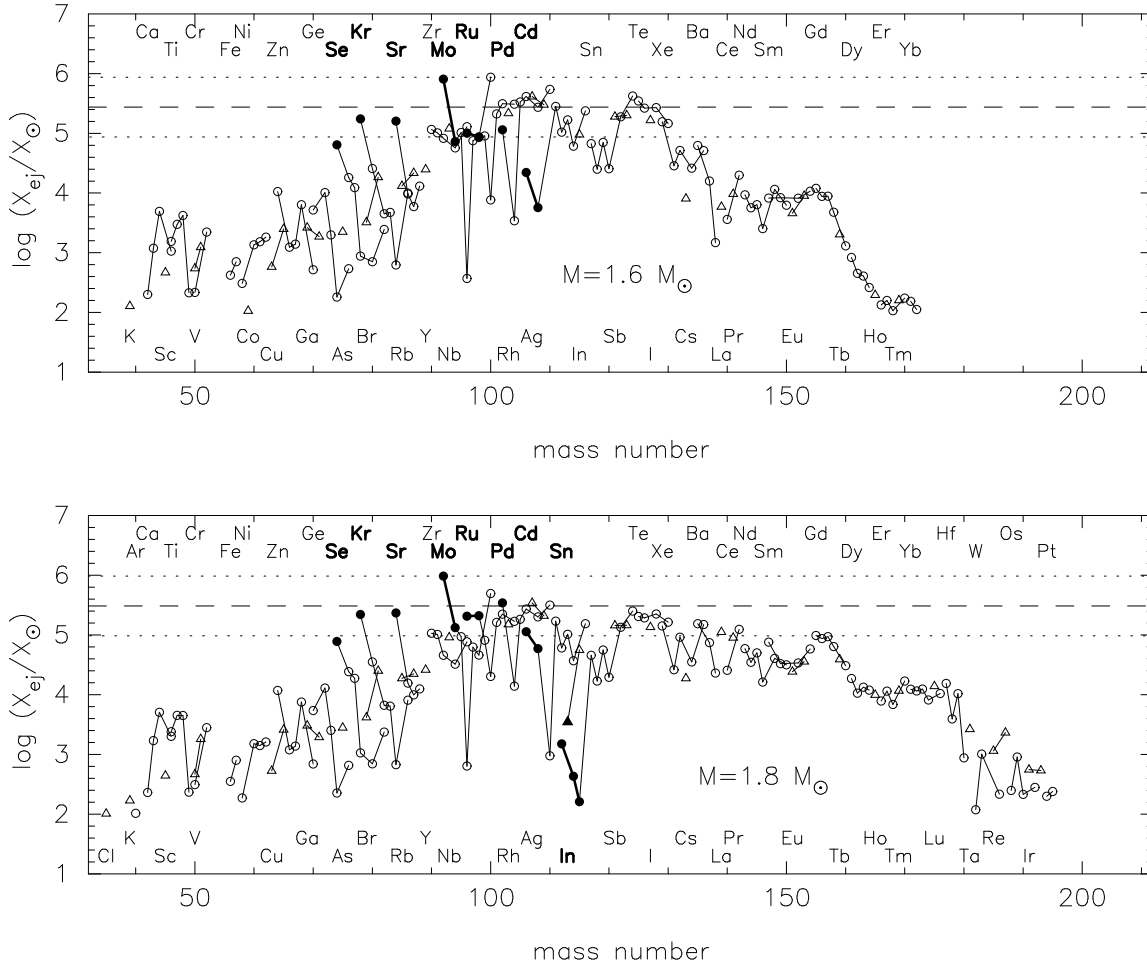


Fig. 16.— Same as Figure 15, but for  $M = 1.6 M_{\odot}$  (top) and  $1.8 M_{\odot}$  (bottom) models.

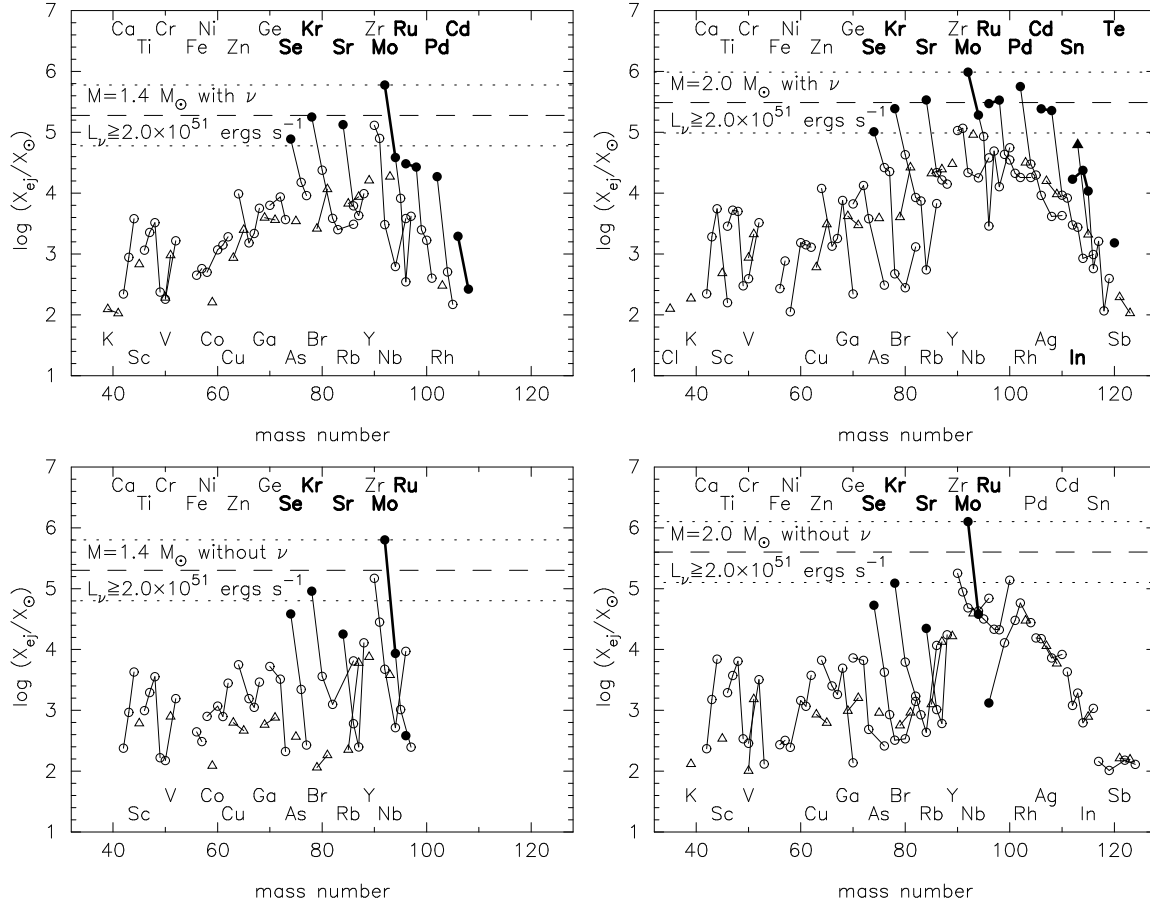


Fig. 17.— Same as Figure 15, but for  $L_{\nu} \geq 2 \times 10^{51} \text{ ergs s}^{-1}$  ( $t_{\text{pb}} \leq 4 \text{ s}$ ). Top and bottom panels show the results with and without neutrino-induced reactions (eqs. [1]-[6]), respectively.

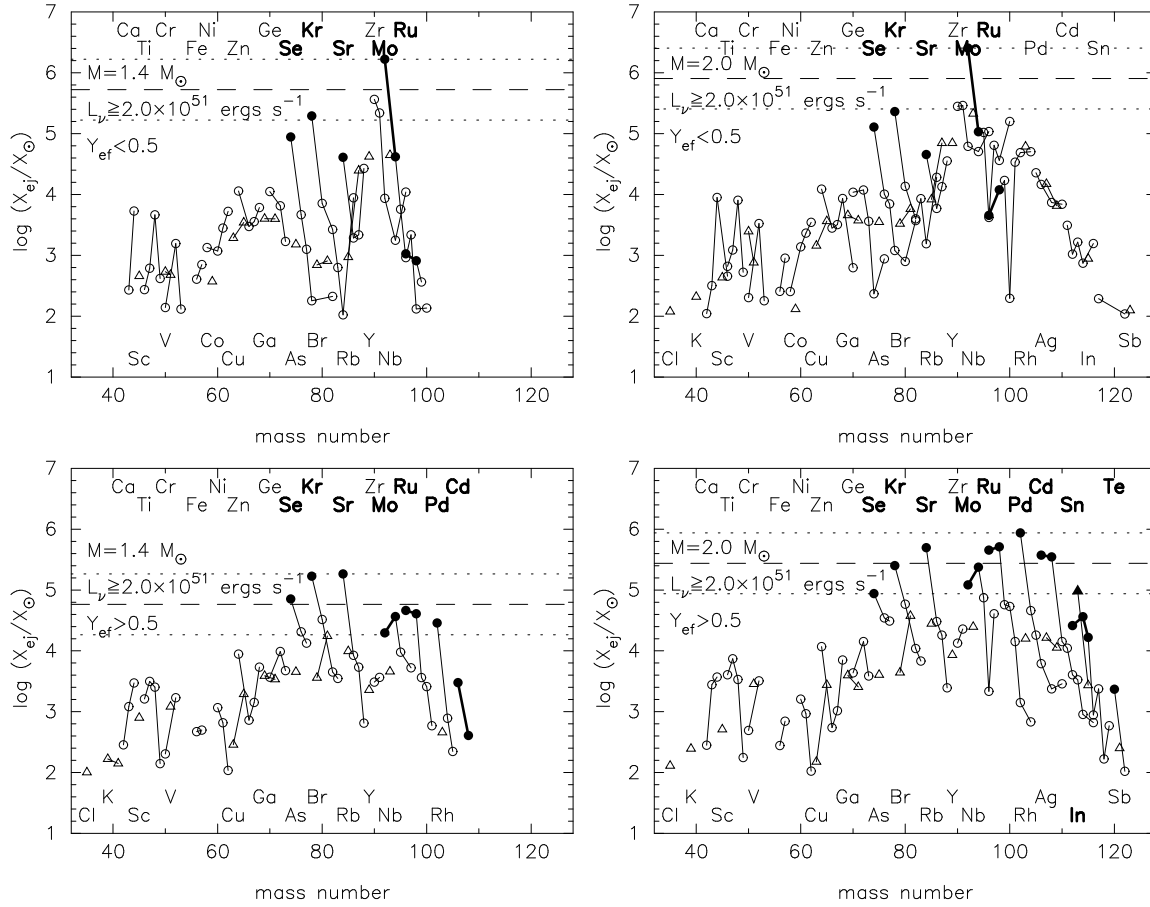


Fig. 18.— Same as Figure 15, but for  $L_{\nu} \geq 2 \times 10^{51} \text{ ergs s}^{-1}$  ( $t_{pb} \leq 4 \text{ s}$ ). Top and bottom panels show the results for the neutron-rich ( $Y_{ef} < 0.5$ ) and proton-rich ( $Y_{ef} > 0.5$ ) winds, respectively.